

Lecture 08 – Intermediate Representation

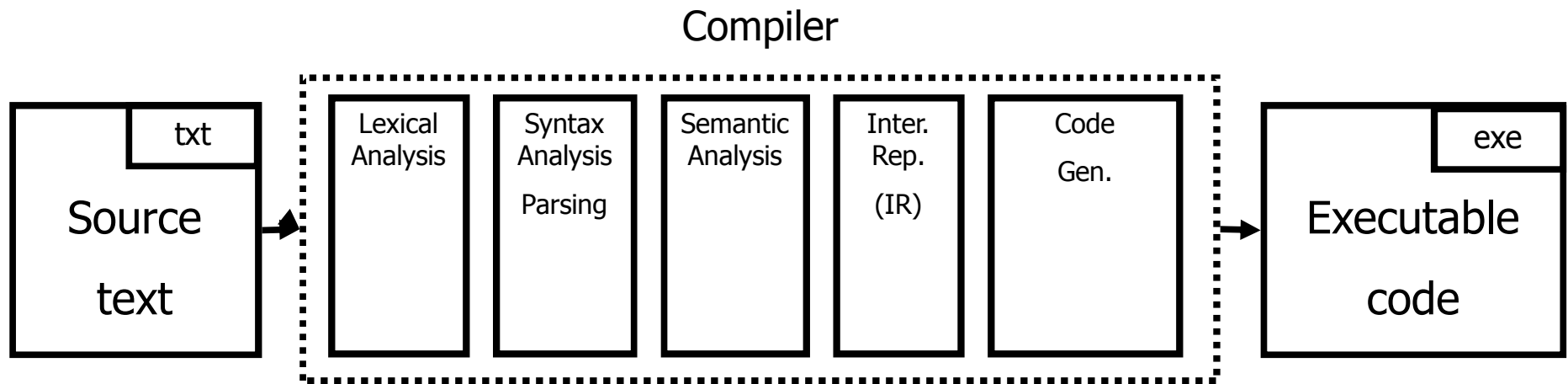
THEORY OF COMPILATION

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www.cs.technion.ac.il/~yahave/tocs2011/compilers-leco8.pptx

Reference: Dragon 6.2,6.3,6.4,6.6

You are here



Last Week: Attribute Grammars

- Adding attributes + actions to a grammar
- Evaluating attributes
 - Build AST
 - Build dependency graph
 - Evaluation based on topological order
 - (works as long as there are no cycles)
- L-attributes, S-attributed grammars
 - Pre-determined evaluation order
 - Can be integrated into parsing

Last Week: Three Address Code (3AC)

- Every instruction operates on three addresses
 - $\text{result} = \text{operand}_1 \text{ operator } \text{operand}_2$
- Close to low-level operations in the machine language
 - Operator is a basic operation
- Statements in the source language may be mapped to multiple instructions in three address code
- can be represented as “quads”
(result, operand₁, operator, operand₂)

Last Week: Creating 3AC

- Assume bottom up parser
 - Covers a wider range of grammars
 - LALR sufficient to cover most programming languages
- Creating 3AC via syntax directed translation
- Attributes
 - code – code generated for a nonterminal
 - var – name of variable that stores result of nonterminal
- freshVar() – helper function that returns the name of a fresh variable

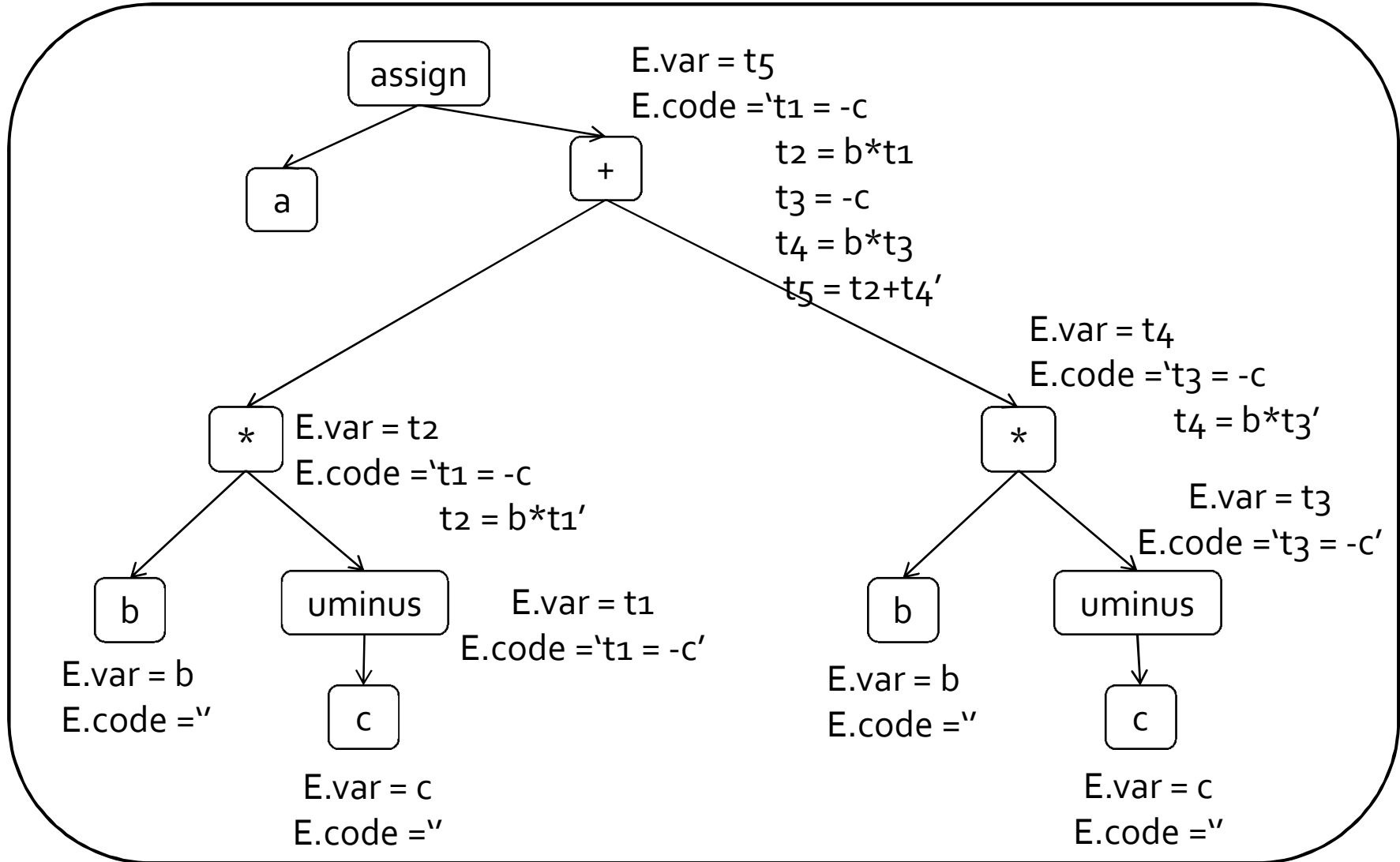
Creating 3AC: expressions

production	semantic rule
$S \rightarrow id := E$	$S.code := E.code \parallel gen(id.var := E.var)$
$E \rightarrow E_1 + E_2$	$E.var := freshVar();$ $E.code = E_1.code \parallel E_2.code \parallel gen(E.var := E_1.var '+' E_2.var)$
$E \rightarrow E_1 * E_2$	$E.var := freshVar();$ $E.code = E_1.code \parallel E_2.code \parallel gen(E.var := E_1.var '*' E_2.var)$
$E \rightarrow - E_1$	$E.var := freshVar();$ $E.code = E_1.code \parallel gen(E.var := 'uminu' E_1.var)$
$E \rightarrow (E_1)$	$E.var := E_1.var$ $E.code = '(' \parallel E_1.code \parallel ')'$
$E \rightarrow id$	$E.var := id.var; E.code = ''$

(we use \parallel to denote concatenation of intermediate code fragments)

example

$$a = b * -c + b * -c$$



Three address code: example

```
int main(void) {  
    int i;  
    int b[10];  
    for (i = 0; i < 10; ++i)  
        b[i] = i*i;  
}
```

```
i := 0 ; assignment  
L1: if i >= 10 goto L2 ; conditional jump  
    t0 := i*i  
    t1 := &b ; address-of operation  
    t2 := t1 + i ; t2 holds the address of b[i]  
    *t2 := t0 ; store through pointer  
    i := i + 1  
    goto L1  
L2:
```


Static Single-Assignment Form (SSA)

- Every assignment writes to a distinct variable
- Every variable is only assigned once

```
p = a + b
```

```
q = p - c
```

```
p = q * d
```

```
p = e - p
```

```
q = p + q
```

```
p1 = a + b
```

```
q1 = p1 - c
```

```
p2 = q1 * d
```

```
p3 = e - p2
```

```
q2 = p3 + q1
```

SSA

```
if (f)
  x = 42;
else
  x = 73;
y = x * a;
```

```
if (f)
  x1 = 42;
else
  x2 = 73;
x3 =  $\phi(x1, x2)$ ;
y = x3 * a;
```

- ϕ (phi) function combines different definitions
- ϕ returns the value of $x1$ if control passes through the true branch and the value of $x2$ if it passed through the false branch

SSA why should we care?

```
x = 42
```

```
x = 73
```

```
y = x
```

```
x1 = 42
```

```
x2 = 73
```

```
y = x2
```

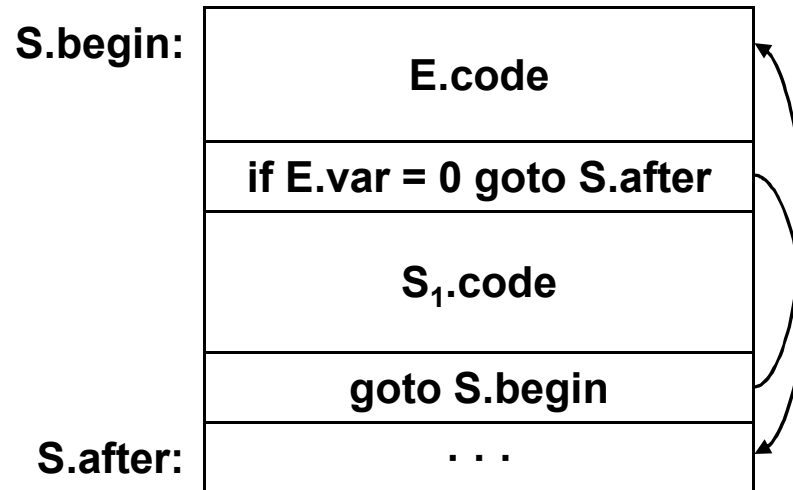
- makes it easy to apply many optimizations
 - constant propagation, dead code elimination...

Creating 3AC: control statements

- 3AC only supports conditional/unconditional jumps
- Add labels
- Attributes
 - begin – label marks beginning of code
 - after – label marks end of code
- Helper function `freshLabel()` allocates a new fresh label

Creating 3AC: control statements

$S \rightarrow \text{while } E \text{ do } S_1$



production	semantic rule
$S \rightarrow \text{while } E \text{ do } S_1$	$S.\text{begin} := \text{freshLabel}();$ $S.\text{after} = \text{freshLabel}();$ $S.\text{code} :=$ $\text{gen}(S.\text{begin} \text{ ':'}) \parallel E.\text{code} \parallel$ $\text{gen}(\text{'if' } E.\text{var} \text{ '=' '0' 'goto' } S.\text{after}) \parallel$ $S_1.\text{code} \parallel \text{gen}(\text{'goto' } S.\text{begin}) \parallel \text{gen}(S.\text{after} \text{ ':'})$

Allocating Memory

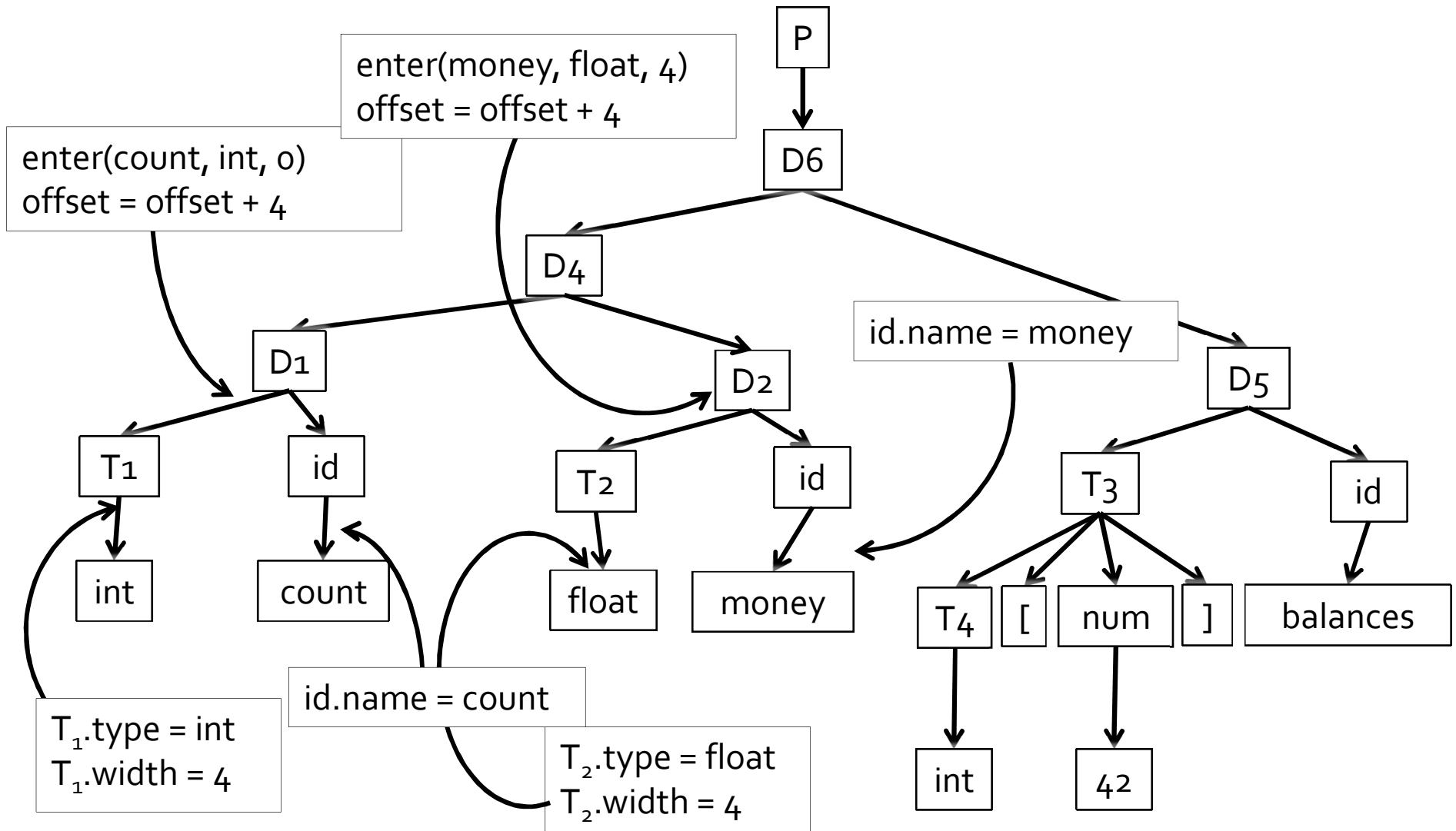
- Type checking helped us guarantee correctness
- Also tells us
 - How much memory allocate on the heap/stack for variables
 - Where to find variables (based on offsets)
 - Compute address of an element inside array (size of stride based on type of element)

Allocating Memory

- Global variable “offset” with memory allocated so far

production	semantic rule
$P \rightarrow D$	{ offset := 0 }
$D \rightarrow D D$	
$D \rightarrow T \text{ id};$	{ enter(id.name, T.type, offset); offset += T.width }
$T \rightarrow \text{integer}$	{ T.type := int; T.width = 4 }
$T \rightarrow \text{float}$	{ T.type := float; T.width = 8 }
$T \rightarrow T_1[\text{num}]$	{ T.type = array (num.val, T1.Type); T.width = num.val * T1.width; }
$T \rightarrow *T_1$	{ T.type := pointer(T1.type); T.width = 4 }

Allocating Memory



Adjusting to bottom-up

production	semantic rule
$P \rightarrow M D$	
$M \rightarrow \varepsilon$	{ offset := o }
$D \rightarrow D D$	
$D \rightarrow T \text{ id};$	{ enter(id.name, T.type, offset); offset += T.width }
$T \rightarrow \text{integer}$	{ T.type := int; T.width = 4 }
$T \rightarrow \text{float}$	{ T.type := float; T.width = 8 }
$T \rightarrow T_1[\text{num}]$	{ T.type = array (num.val, T1.Type); T.width = num.val * T1.width; }
$T \rightarrow *T_1$	{ T.type := pointer(T1.type); T.width = 4 }

Generating IR code

- Option 1
accumulate code in AST attributes
- Option 2
emit IR code to a file during compilation
 - If for every production the code of the left-hand-side is constructed from a concatenation of the code of the RHS in some fixed order

Expressions and assignments

production	semantic action
$S \rightarrow id := E$	{ p:= lookup(id.name); if p \neq null then emit (p $:=$ ' E.var) else error }
$E \rightarrow E_1 \text{ op } E_2$	{ E.var := freshVar(); emit (E.var $:=$ E1.var op E2.var) }
$E \rightarrow - E_1$	{ E.var := freshVar(); emit (E.var $:=$ 'uminus' E1.var) }
$E \rightarrow (E_1)$	{ E.var := E1.var }
$E \rightarrow id$	{ p:= lookup(id.name); if p \neq null then E.var :=p else error }

Boolean Expressions

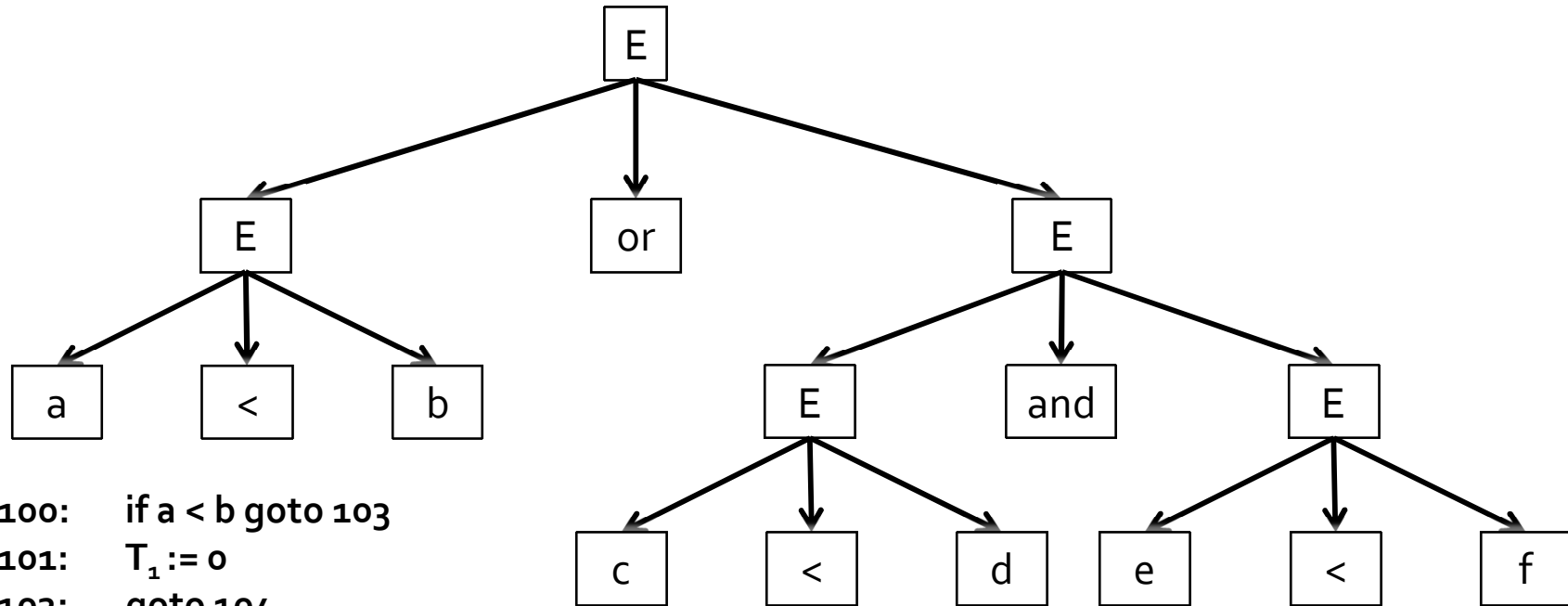
production	semantic action
$E \rightarrow E_1 \text{ op } E_2$	{ E.var := freshVar(); emit(E.var := ' E1.var op E2.var) } }
$E \rightarrow \text{not } E_1$	{ E.var := freshVar(); emit(E.var := 'not' E1.var) } }
$E \rightarrow (E_1)$	{ E.var := E1.var }
$E \rightarrow \text{true}$	{ E.var := freshVar(); emit(E.var := '1') }
$E \rightarrow \text{false}$	{ E.var := freshVar(); emit(E.var := '0') }

- Represent true as 1, false as 0
- Wasteful representation, creating variables for true/false

Boolean expressions via jumps

production	semantic action
$E \rightarrow id_1 \text{ op } id_2$	<pre>{ E.var := freshVar(); emit('if' id1.var relop id2.var 'goto' nextStmt+2); emit(E.var := '0'); emit('goto ` nextStmt + 1); emit(E.var := '1') }</pre>

Example



100: if a < b goto 103
101: $T_1 := 0$
102: goto 104
103: $T_1 := 1$

104: if c < d goto 107
105: $T_2 := 0$
106: goto 108
107: $T_2 := 1$

108: if e < f goto 111
109: $T_3 := 0$
110: goto 112
111: $T_3 := 1$
112: $T_4 := T_2 \text{ and } T_3$
113: $T_5 := T_1 \text{ or } T_4$

Short circuit evaluation

- Second argument of a Boolean operator is only evaluated if the first argument does not already determine the outcome
- $(x \text{ and } y)$ is equivalent to `if x then y else false;`
- $(x \text{ or } y)$ is equivalent to `if x then true else y`

example

$a < b$ or $(c < d$ and $e < f)$

```
100: if a < b goto 103
101: T1 := 0
102: goto 104
103: T1 := 1
104: if c < d goto 107
105: T2 := 0
106: goto 108
107: T2 := 1
108: if e < f goto 111
109: T3 := 0
110: goto 112
111: T3 := 1
112: T4 := T2 and T3
113: T5 := T1 and T4
```

naive

```
100: if a < b goto 105
101: if !(c < d) goto 103
102: if e < f goto 105
103: T := 0
104: goto 106
105: T := 1
106:
```

Short circuit evaluation

More examples

- if (x != null && x.val = 42)

```
int denom = 0;
if (denom && nom/denom) {
    oops_i_just_divided_by_zero();
}
```

```
int x=0;
if (++x>0 && x++) {
    hmmm();
}
```

Control Structures

```
S → if B then S1  
   | if B then S1 else S2  
   | while B do S1
```

- For every Boolean expression B, we attach two properties
 - falseLabel – target label for a jump when condition B evaluates to false
 - trueLabel – target label for a jump when condition B evaluates to true
- For every statement we attach a property
 - S.next – the label of the next code to execute after S
- Challenge
 - Compute falseLabel and trueLabel during code generation

Control Structures: next

production	semantic action
$P \rightarrow S$	$S.next = \text{freshLabel}();$ $P.code = S.code \parallel \text{label}(S.next)$
$S \rightarrow S_1S_2$	$S_1.next = \text{freshLabel}();$ $S_2.next = S.next;$ $S.code = S_1.code \parallel \text{label}(S_1.next) \parallel S_2.code$

- Is $S.next$ inherited or synthesized?
- Is $S.code$ inherited or synthesized?

- The label $S.next$ is symbolic, we will only determine its value after we finish deriving S

Control Structures: conditional

production	semantic action
$S \rightarrow \text{if } B \text{ then } S_1$	<pre>B.trueLabel = freshLabel(); B.falseLabel = S.next; S1.next = S.next; S.code = B.code gen (B.trueLabel ':') S1.code</pre>

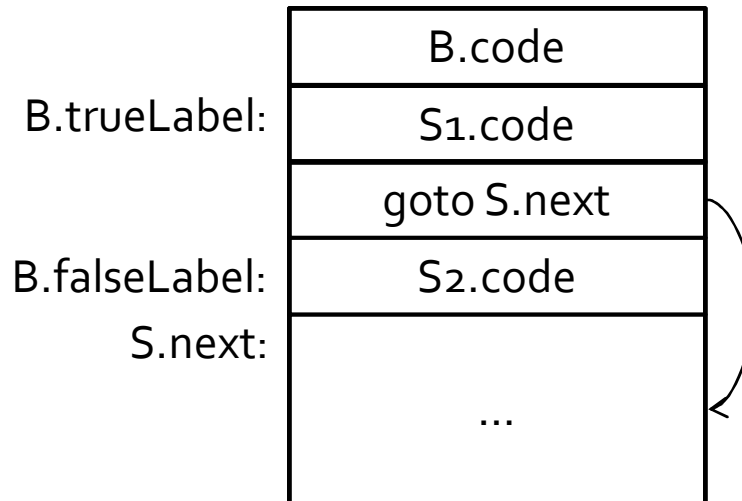
- Are $S_1.next$, $B.falseLabel$ inherited or synthesized?
- Is $S.code$ inherited or synthesized?

Control Structures: conditional

production	semantic action
$S \rightarrow \text{if } B \text{ then } S_1 \text{ else } S_2$	<pre>B.trueLabel = freshLabel(); B.falseLabel = freshLabel(); S1.next = S.next; S2.next = S.next; S.code = B.code gen(B.trueLabel ':') S1.code gen('goto' S.next) gen(B.falseLabel ':') S2.code</pre>

- B.trueLabel and B.falseLabel considered inherited

Control Structures: conditional



```
B.trueLabel = freshLabel();
B.falseLabel = freshLabel();
S1.next = S.next;
S2.next = S.next;
S.code =
  B.code || gen(B.trueLabel `:`) || S1.code || gen(`goto` S.next)
  || gen(B.falseLabel `:`) || S2.code
```

Boolean expressions

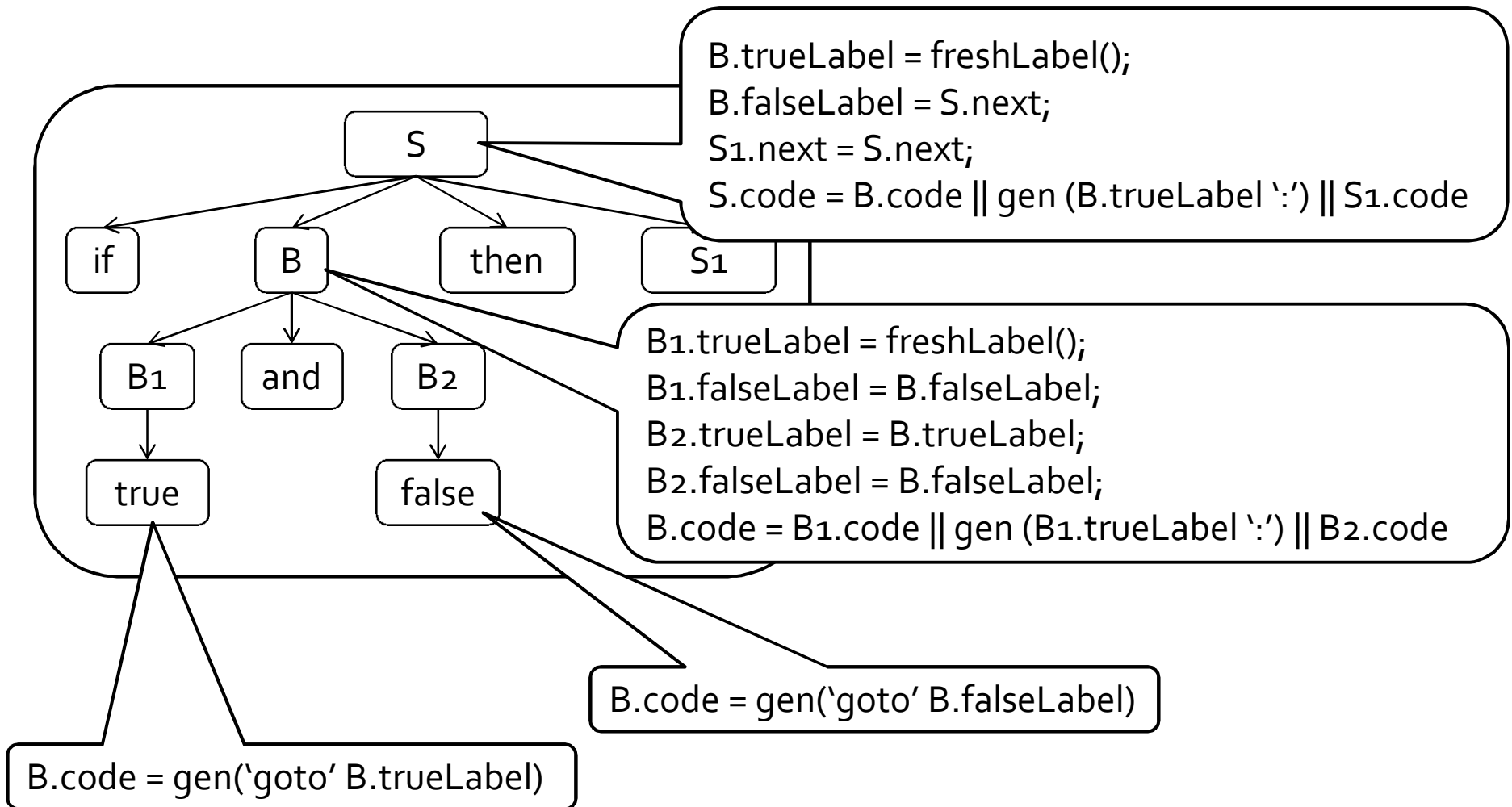
production	semantic action
$B \rightarrow B_1 \text{ or } B_2$	<pre>B1.trueLabel = B.trueLabel; B1.falseLabel = freshLabel(); B2.trueLabel = B.trueLabel; B2.falseLabel = B.falseLabel; B.code = B1.code gen (B1.falseLabel `:`) B2.code</pre>
$B \rightarrow B_1 \text{ and } B_2$	<pre>B1.trueLabel = freshLabel(); B1.falseLabel = B.falseLabel; B2.trueLabel = B.trueLabel; B2.falseLabel = B.falseLabel; B.code = B1.code gen (B1.trueLabel `:`) B2.code</pre>
$B \rightarrow \text{not } B_1$	<pre>B1.trueLabel = B.falseLabel; B1.falseLabel = B.trueLabel; B.code = B1.code;</pre>
$B \rightarrow (B_1)$	<pre>B1.trueLabel = B.trueLabel; B1.falseLabel = B.falseLabel; B.code = B1.code;</pre>
$B \rightarrow \text{id}_1 \text{ relop id}_2$	<pre>B.code=gen (`if' id1.var relop id2.var `goto' B.trueLabel) gen(`goto' B.falseLabel);</pre>
$B \rightarrow \text{true}$	<pre>B.code = gen(`goto' B.trueLabel)</pre>
$B \rightarrow \text{false}$	<pre>B.code = gen(`goto' B.falseLabel);</pre>

Boolean expressions

production	semantic action
$B \rightarrow B_1 \text{ or } B_2$	<pre>B1.trueLabel = B.trueLabel; B1.falseLabel = freshLabel(); B2.trueLabel = B.trueLabel; B.falseLabel = B.falseLabel; B.code = B1.code gen (B1.falseLabel `:`) B2.code</pre>

- How can we determine the address of B_1 .falseLabel?
- Only possible after we know the code of B_1 and all the code preceding B_1

Example



Computing labels

- We can compute the values for the labels but it would require more than one pass on the AST
- Can we do it in a single pass?

Backpatching

- Goal: generate code in a single pass
- Generate code as we did before, but manage labels differently
- Keep labels symbolic until values are known, and then back-patch them
- New synthesized attributes for B
 - B.truelist – list of jump instructions that eventually get the label where B goes when B is true.
 - B.falselist – list of jump instructions that eventually get the label where B goes when B is false.

Backpatching

- For every label, maintain a list of instructions that jump to this label
- When the address of the label is known, go over the list and update the address of the label
- Previous solutions do not guarantee a single pass
 - The attribute grammar we had before is not S-attributed (e.g., next), and is not L-attributed.

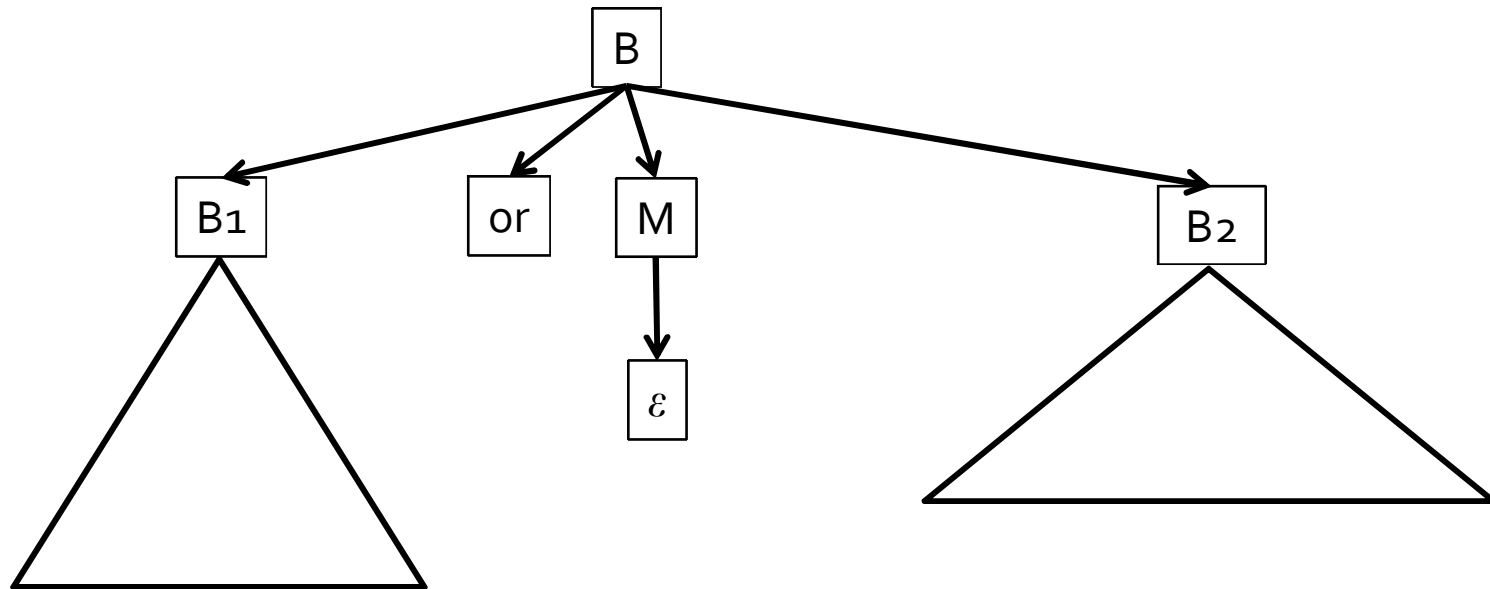
Backpatching

- `makelist(addr)` – create a list of instructions containing `addr`
- `merge(p1,p2)` – concatenate the lists pointed to by `p1` and `p2`, returns a pointer to the new list
- `backpatch(p,addr)` – inserts `i` as the target label for each of the instructions in the list pointed to by `p`

Backpatching Boolean expressions

production	semantic action
$B \rightarrow B_1 \text{ or } M B_2$	<pre>backpatch(B1.falseList,M.instr); B.trueList = merge(B1.trueList,B2.trueList); B.falseList = B2.falseList;</pre>
$B \rightarrow B_1 \text{ and } M B_2$	<pre>backpatch(B1.trueList,M.instr); B.trueList = B2.trueList; B.falseList = merge(B1.falseList,B2.falseList);</pre>
$B \rightarrow \text{not } B_1$	<pre>B.trueList = B1.falseList; B.falseList = B1.trueList;</pre>
$B \rightarrow (B_1)$	<pre>B.trueList = B1.trueList; B.falseList = B1.falseList;</pre>
$B \rightarrow \text{id}_1 \text{ relop id}_2$	<pre>B.trueList = makeList(nextInstr); B.falseList = makeList(nextInstr+1); emit('if' id1.var relop id2.var 'goto _') emit('goto _');</pre>
$B \rightarrow \text{true}$	<pre>B.trueList = makeList(nextInstr); emit('goto _');</pre>
$B \rightarrow \text{false}$	<pre>B.falseList = makeList(nextInstr); emit('goto _');</pre>
$M \rightarrow \epsilon$	<pre>M.instr = nextinstr;</pre>

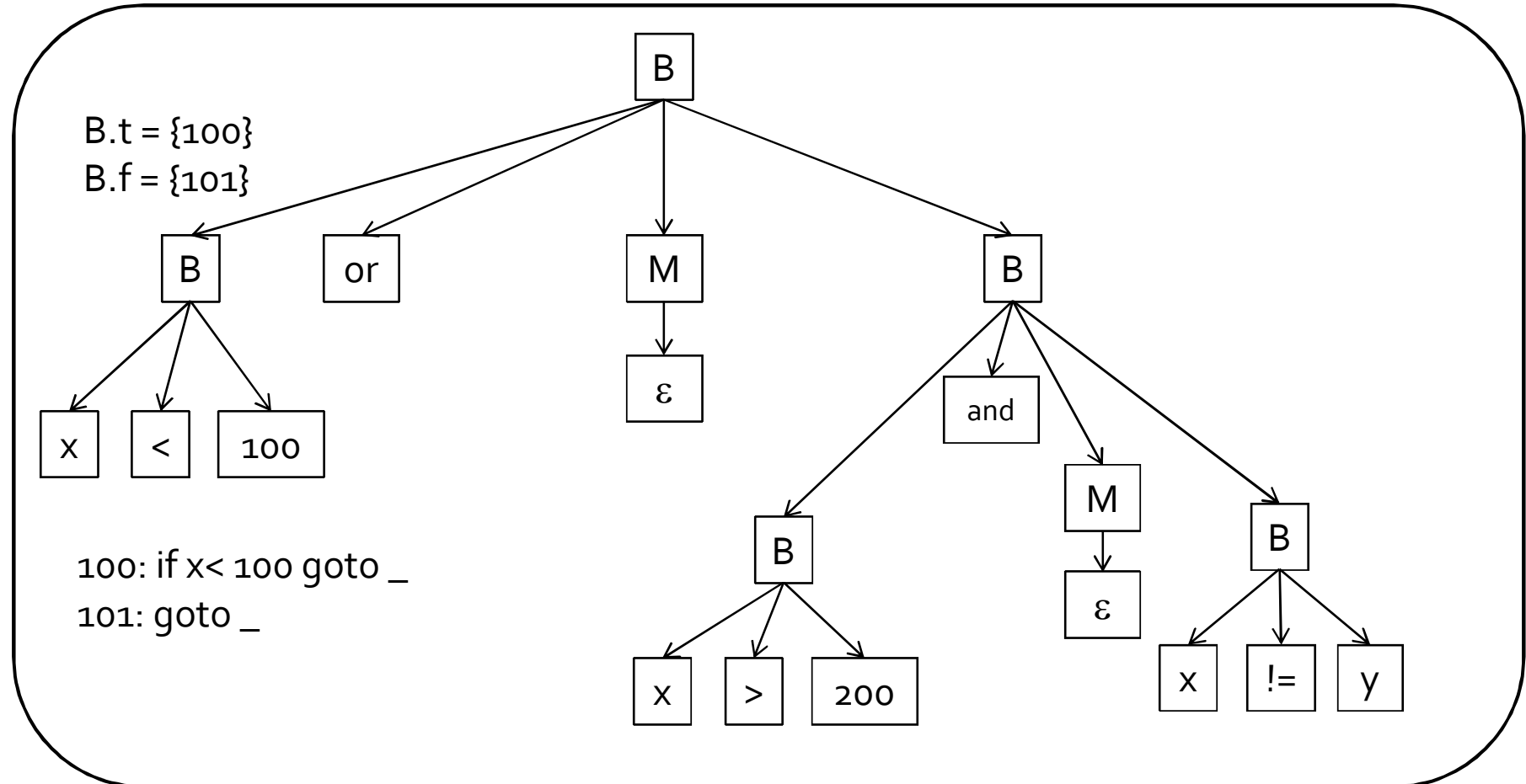
Marker



- { M.instr = nextinstr; }
- Use M to obtain the address just before B2 code starts being generated

Example

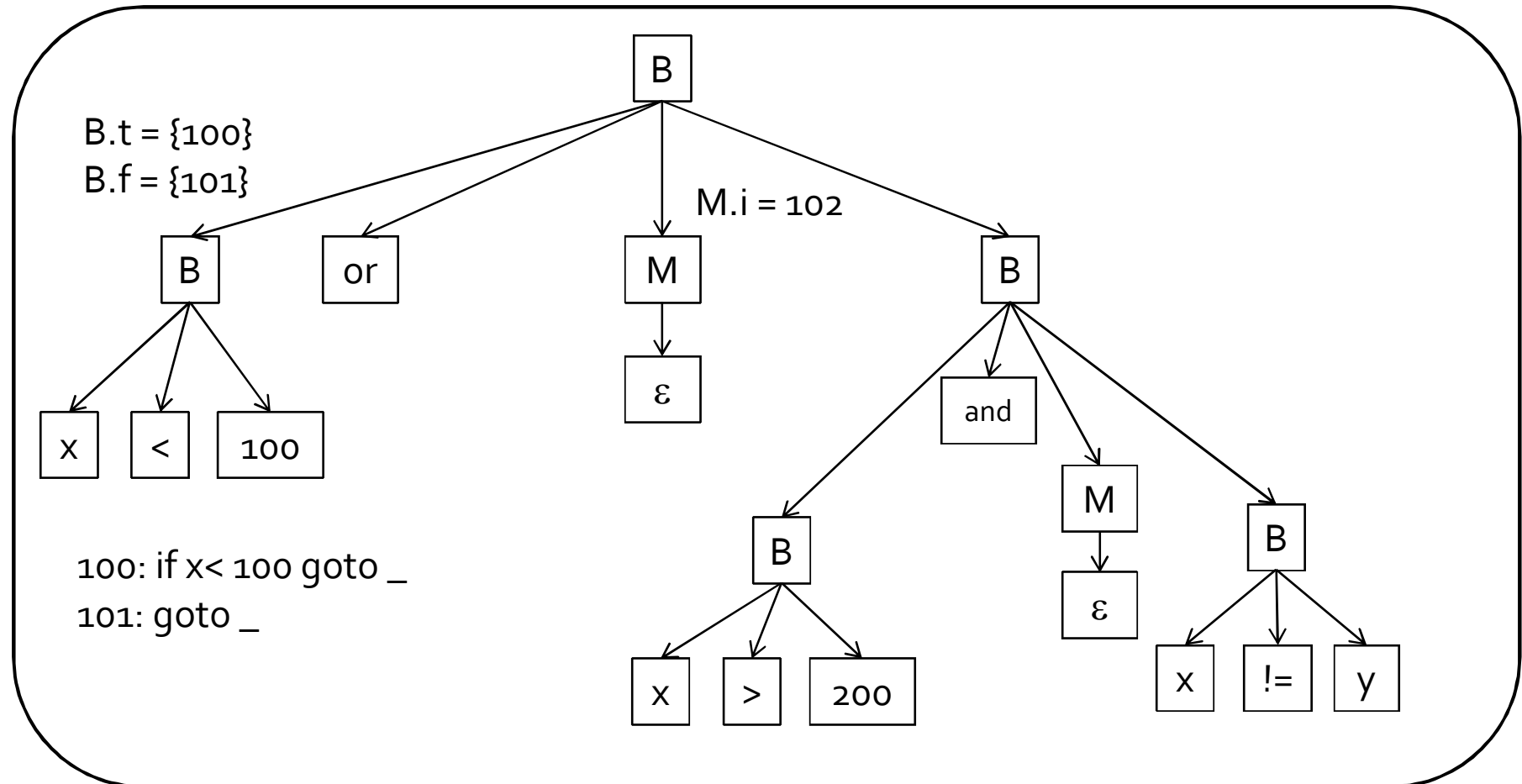
$X < 100$ or $x > 200$ and $x \neq y$



$B \rightarrow id_1 \text{ relop } id_2$	$B.trueList = makeList(nextInstr);$ $B.falseList = makeList(nextInstr+1);$ $emit('if' id_1.var \text{ relop } id_2.var 'goto _') \parallel emit('goto _');$
--	---

Example

$X < 100$ or $x > 200$ and $x \neq y$

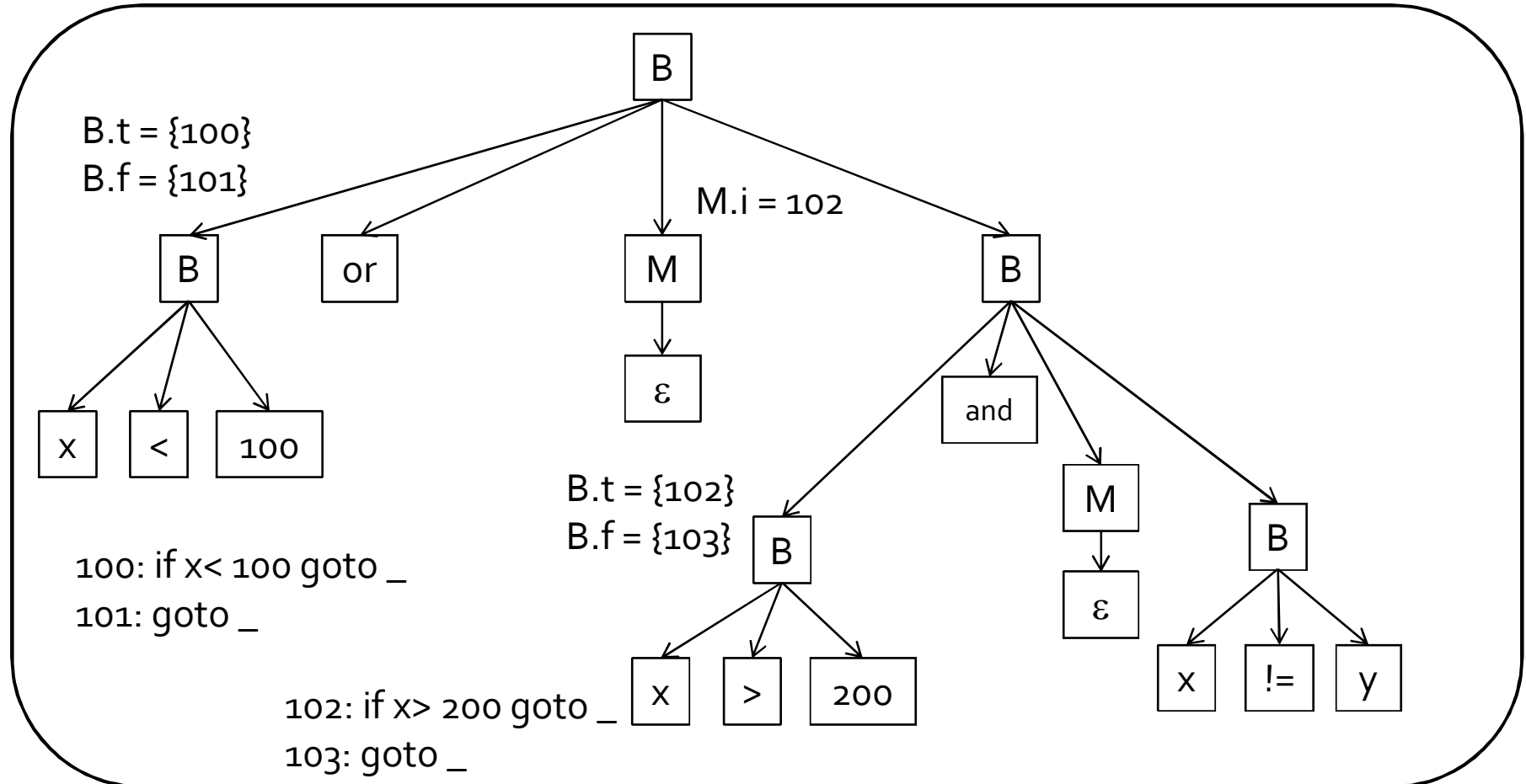


$M \rightarrow \epsilon$

$M.instr = \text{nextinstr};$

Example

$X < 100$ or $x > 200$ and $x \neq y$



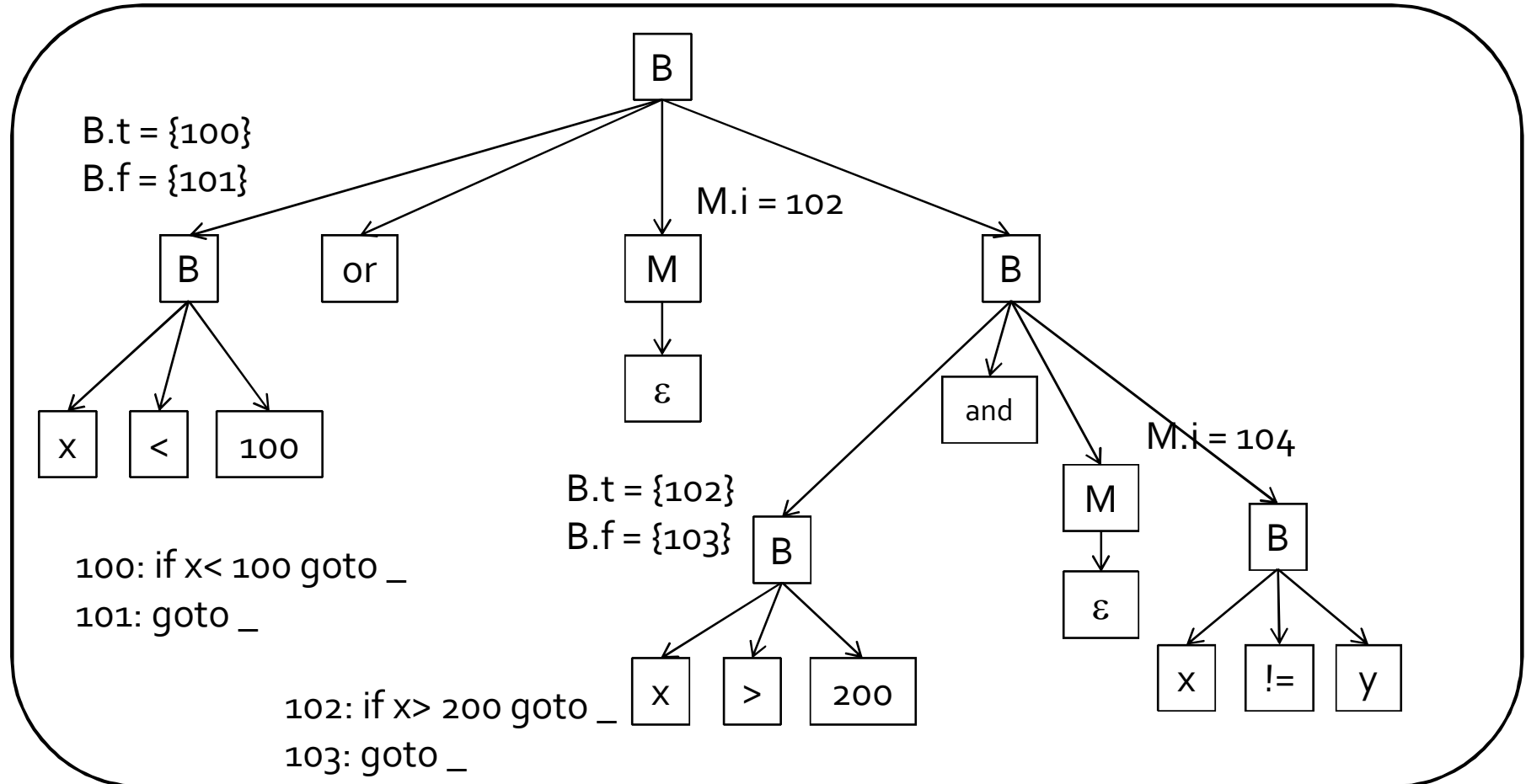
$B \rightarrow id_1 \text{ relop } id_2$

```

B.trueList = makeList(nextInstr);
B.falseList = makeList(nextInstr+1);
emit ('if' id1.var relop id2.var 'goto _') || emit('goto _');
  
```

Example

$X < 100$ or $x > 200$ and $x \neq y$

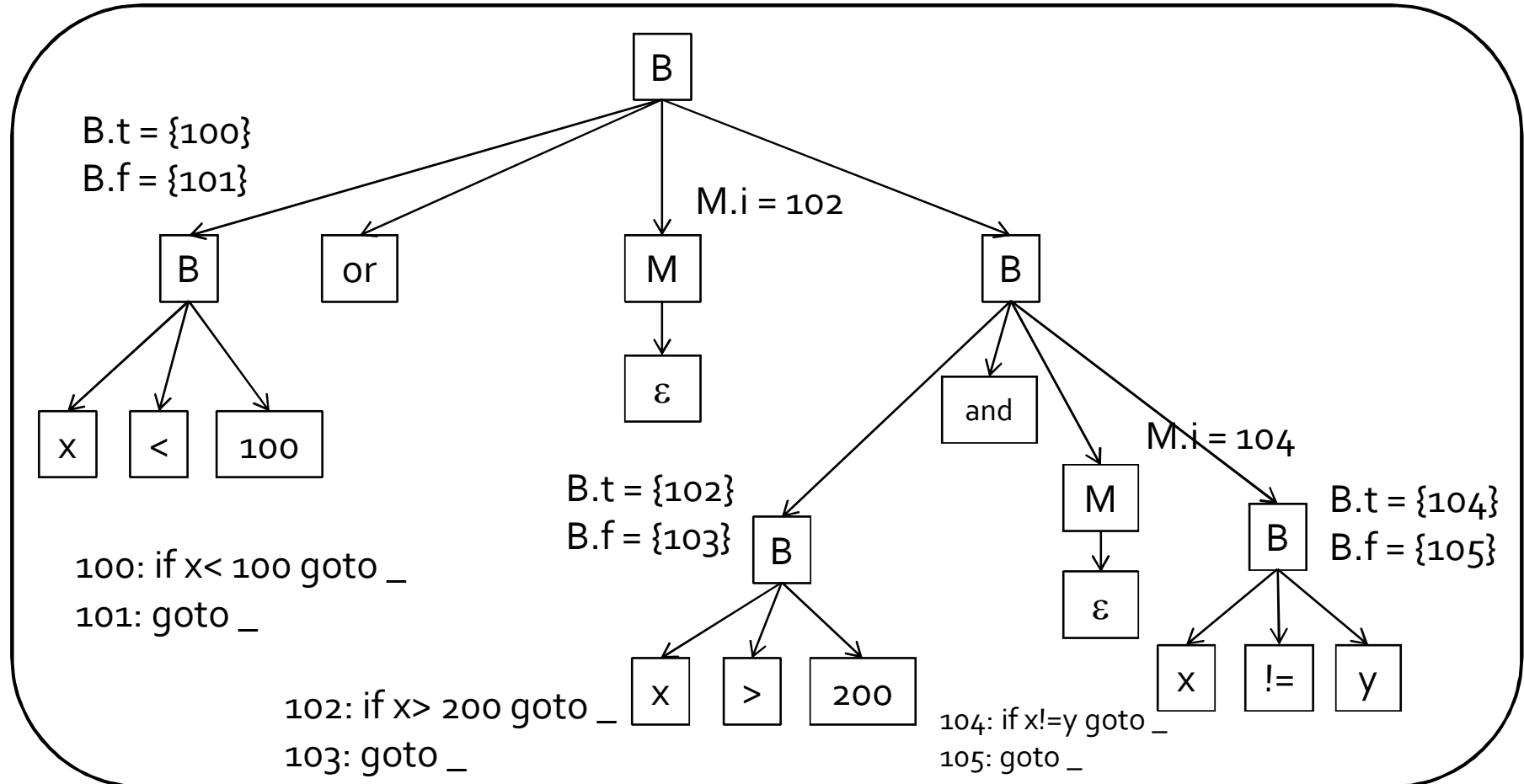


$M \rightarrow \epsilon$

$M.instr = nextinstr;$

Example

$X < 100$ or $x > 200$ and $x \neq y$



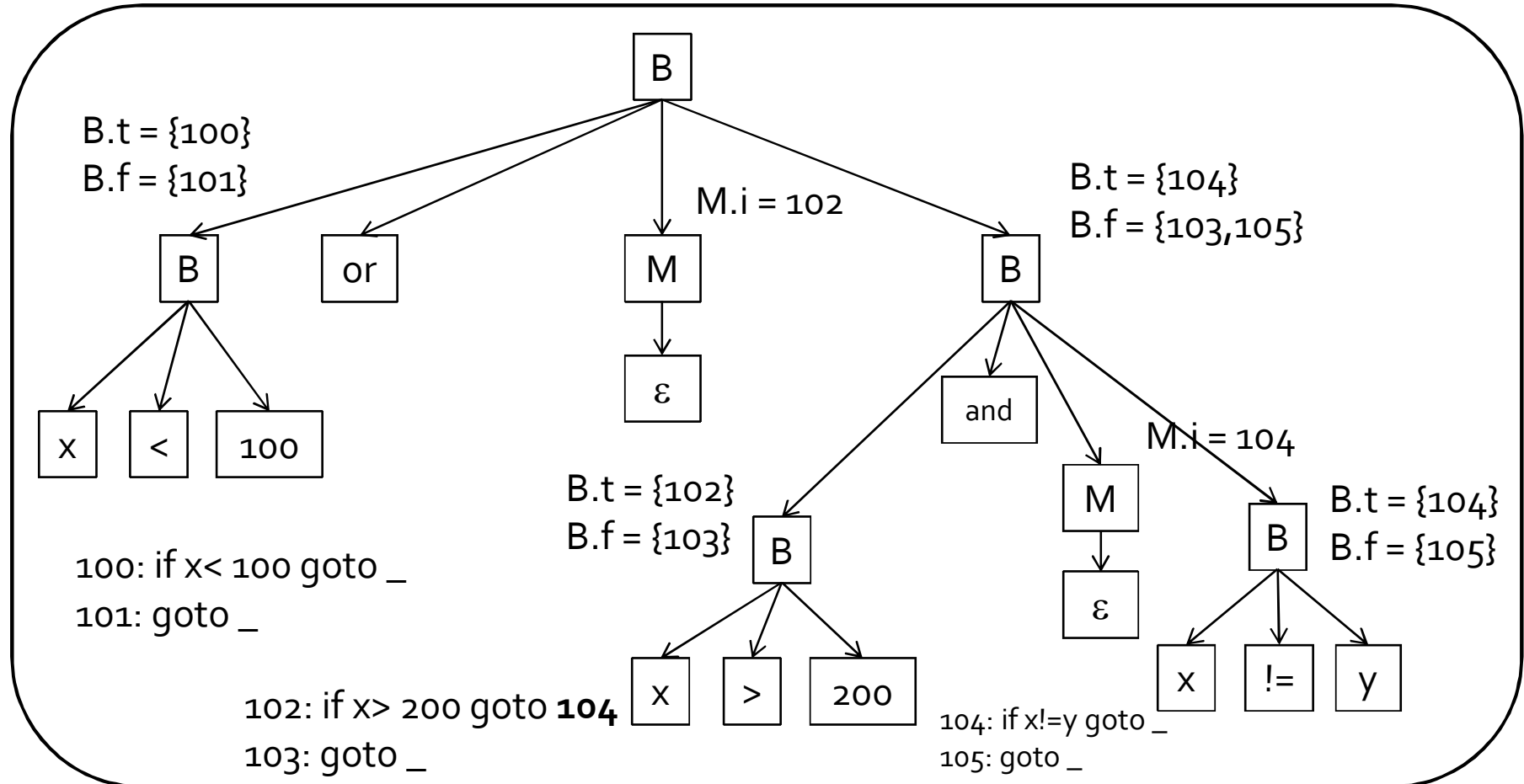
$B \rightarrow id_1 \text{ relop } id_2$

```

B.trueList = makeList(nextInstr);
B.falseList = makeList(nextInstr+1);
emit ('if' id1.var relop id2.var 'goto _') || emit('goto _');
  
```

Example

$X < 100$ or $x > 200$ and $x \neq y$

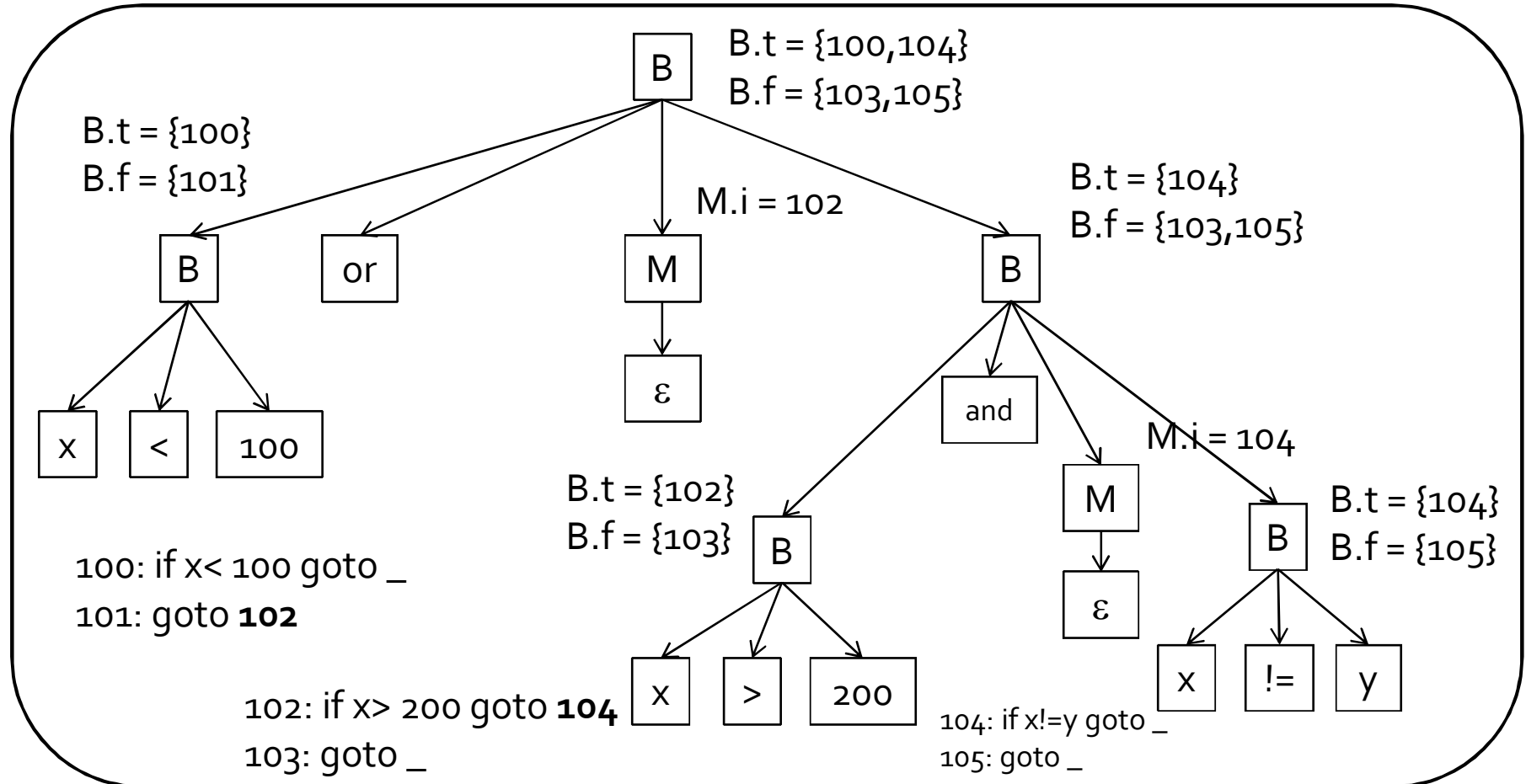


B \rightarrow **B1** and **M B2**

```
backpatch(B1.trueList, M.instr);
B.trueList = B2.trueList;
B.falseList = merge(B1.falseList, B2.falseList);
```

Example

$X < 100$ or $x > 200$ and $x \neq y$



$B \rightarrow B_1$ or $M B_2$

```
backpatch(B1.falseList, M.instr);
B.trueList = merge(B1.trueList, B2.trueList);
B.falseList = B2.falseList;
```

Example

```
100: if x<100 goto _  
101: goto _  
102: if x>200 goto _  
103: goto _  
104: if x!=y goto _  
105: goto _
```

Before backpatching

```
100: if x<100 goto _  
101: goto _  
102: if x>200 goto 104  
103: goto _  
104: if x!=y goto _  
105: goto _
```

After backpatching
by the production
 $B \rightarrow B_1$ and $M B_2$

```
100: if x<100 goto _  
101: goto 102  
102: if x>200 goto 104  
103: goto _  
104: if x!=y goto _  
105: goto _
```

After backpatching
by the production
 $B \rightarrow B_1$ or $M B_2$

Backpatching for statements

production	semantic action
$S \rightarrow \text{if } (B) M S_1$	backpatch(B.trueList,M.instr); S.nextList = merge(B.falseList,S1.nextList);
$S \rightarrow \text{if } (B) M_1 S_1$ $N \text{ else } M_2 S_2$	backpatch(B.trueList,M1.instr); backpatch(B.falseList,M2.instr); temp = merge(S1.nextList,N.nextList); S.nextList = merge(temp,S2.nextList);
$S \rightarrow \text{while } M_1 (B)$ $M_2 S_1$	backpatch(S1.nextList,M1.instr); backpatch(B.trueList,M2.instr); S.nextList = B.falseList; emit('goto' M1.instr);
$S \rightarrow \{ L \}$	S.nextList = L.nextList;
$S \rightarrow A$	S.nextList = null;
$M \rightarrow \epsilon$	M.instr = nextinstr;
$N \rightarrow \epsilon$	N.nextList = makeList(nextInstr); emit('goto _');
$L \rightarrow L_1 M S$	backpatch(L1.nextList,M.instr); L.nextList = S.nextList;
$L \rightarrow S$	L.nextList = S.nextList

Procedures

```
n = f(a[i]);
```

```
t1 = i * 4  
t2 = a[t1] // could have expanded this as well  
param t2  
t3 = call f, 1  
n = t3
```

- we will see handling of procedure calls in much more detail later

Procedures

```
D → define T id (F) { S }  
F → ε | T id, F  
S → return E; | ...  
E → id (A) | ...  
A → ε | E, A
```

statements

expressions

- type checking
 - function type: return type, type of formal parameters
 - within an expression function treated like any other operator
- symbol table
 - parameter names

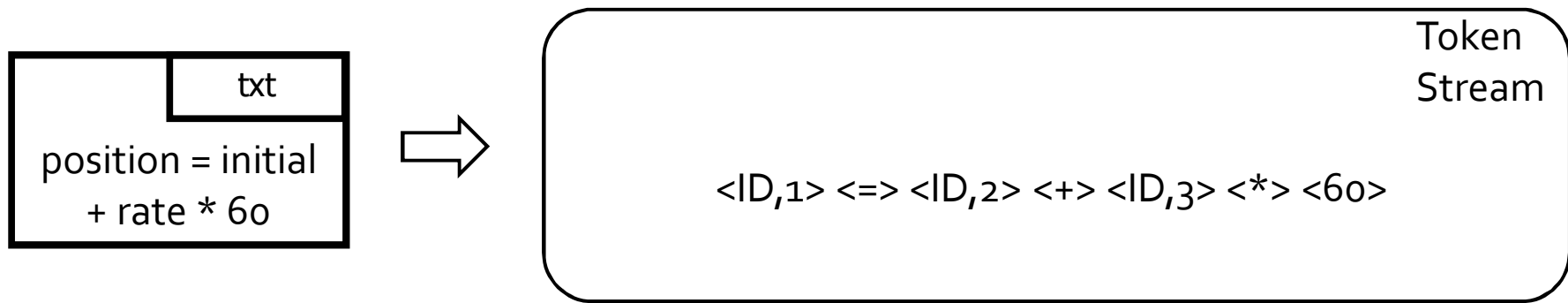
Summary

- pick an intermediate representation
- translate expressions
- use a symbol table to implement declarations
- generate jumping code for boolean expressions
 - value of the expression is implicit in the control location
- backpatching
 - a technique for generating code for boolean expressions and statements in one pass
 - idea: maintain lists of incomplete jumps, where all jumps in a list have the same target. When the target becomes known, all instructions on its list are “filled in”.

Recap

- Lexical analysis
 - regular expressions identify tokens (“words”)
- Syntax analysis
 - context-free grammars identify the structure of the program (“sentences”)
- Contextual (semantic) analysis
 - type checking defined via typing judgements
 - can be encoded via attribute grammars
- Syntax directed translation
 - attribute grammars
- Intermediate representation
 - many possible IRs
 - generation of intermediate representation

Journey inside a compiler

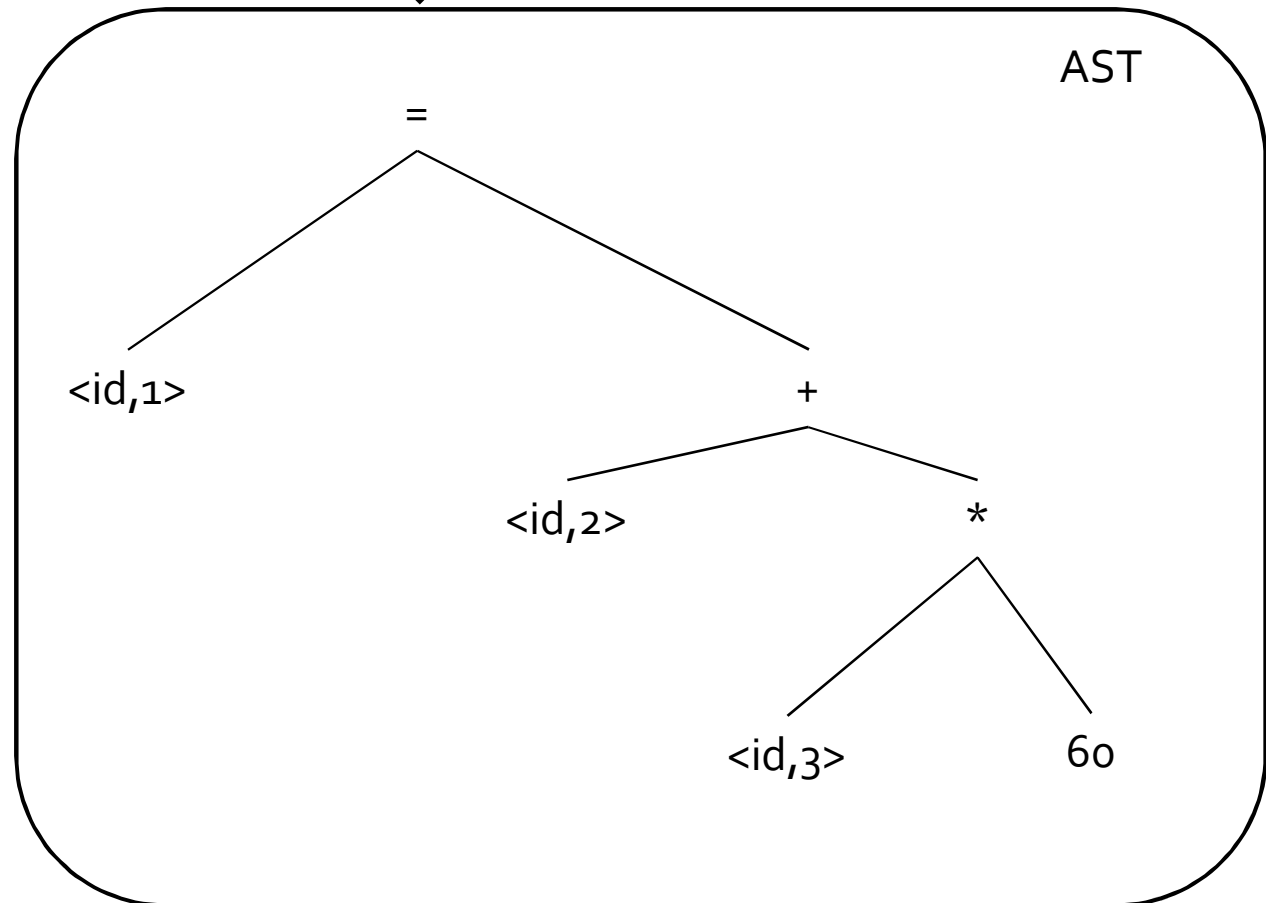


Journey inside a compiler

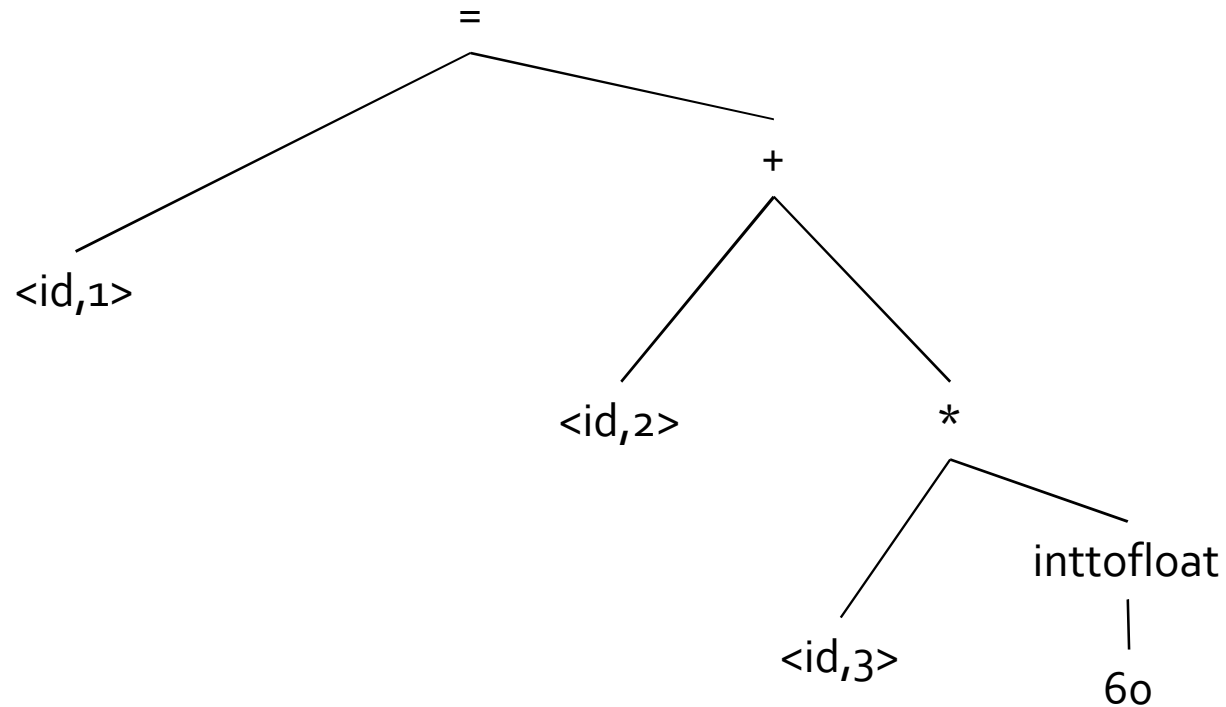
<ID,1> <=> <ID,2> <+> <ID,3> <*> <60>



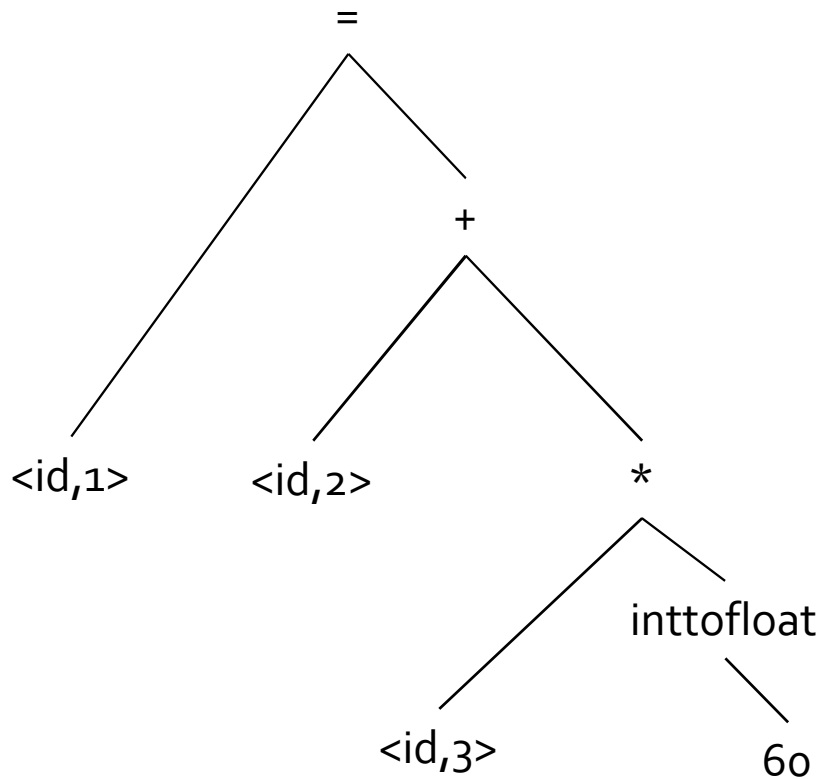
symbol	type	data
position	float	...
initial	float	...
rate	float	...



Journey inside a compiler



Journey inside a compiler



Intermediate
Representation

```
t1 = inttofloat(60)
t2 = id3 * t1
t3 = id2 + t2
id1 = t3
```



Journey inside a compiler

Intermediate
Representation

```
t1 = inttofloat(60)
t2 = id3 * t1
t3 = id2 + t2
id1 = t3
```

Optimized

```
t1 = id3 * 60.0
id1 = id2 + t1
```

Lexical
Analysis

Syntax
Analysis

Sem.
Analysis

Inter.
Rep.

Code
Gen.

Journey inside a compiler

Optimized

```
t1 = id3 * 60.0  
id1 = id2 + t1
```

Code Gen

```
LDF R2, id3  
MULF R2, R2, #60.0  
LDF R1, id2  
ADDF R1, R1, R2  
STF id1, R1
```

Lexical
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Next time

- Runtime Environments

The End