

Lecture 08 – Intermediate Representation

THEORY OF COMPILATION

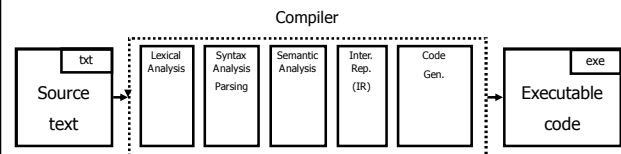
EranYahav

www.cs.technion.ac.il/~yahave/tocs2011/compiler-lec08.pptx

Reference: Dragon 6.2,6.3,6.4,6.6

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You are here



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Last Week: Attribute Grammars

- Adding attributes + actions to a grammar
- Evaluating attributes
 - Build AST
 - Build dependency graph
 - Evaluation based on topological order
 - (works as long as there are no cycles)
- L-attributes, S-attributed grammars
 - Pre-determined evaluation order
 - Can be integrated into parsing

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Last Week: Three Address Code (3AC)

- Every instruction operates on three addresses
 - $result = operand_1 \text{ operator } operand_2$
- Close to low-level operations in the machine language
 - Operator is a basic operation
- Statements in the source language may be mapped to multiple instructions in three address code
- can be represented as "quads" ($result, operand_1, operator, operand_2$)

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Last Week: Creating 3AC

- Assume bottom up parser
 - Covers a wider range of grammars
 - LALR sufficient to cover most programming languages
- Creating 3AC via syntax directed translation
- Attributes
 - code – code generated for a nonterminal
 - var – name of variable that stores result of nonterminal
- freshVar() – helper function that returns the name of a fresh variable

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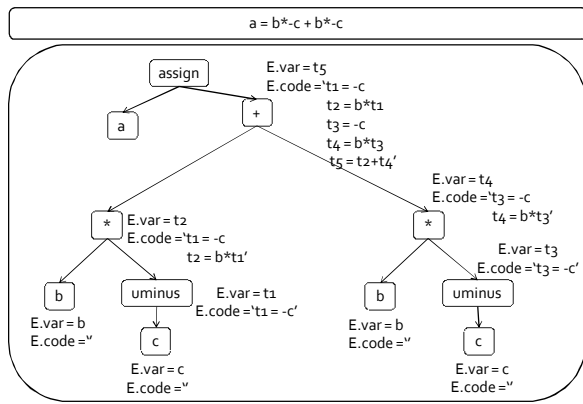
Creating 3AC: expressions

production	semantic rule
$S \rightarrow id := E$	$S.code := E.code \parallel gen(id.var := 'E.var)$
$E \rightarrow E_1 + E_2$	$E.var := freshVar();$ $E.code = E_1.code \parallel E_2.code \parallel gen(E.var := 'E_1.var '+' E_2.var)$
$E \rightarrow E_1 * E_2$	$E.var := freshVar();$ $E.code = E_1.code \parallel E_2.code \parallel gen(E.var := 'E_1.var '*' E_2.var)$
$E \rightarrow - E_1$	$E.var := freshVar();$ $E.code = E_1.code \parallel gen(E.var := 'uminu' E_1.var)$
$E \rightarrow (E_1)$	$E.var := E_1.var$ $E.code = '(' \parallel E_1.code \parallel ')'$
$E \rightarrow id$	$E.var := id.var; E.code = ''$

(we use || to denote concatenation of intermediate code fragments)

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example



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Three address code: example

```
int main(void) {
    int i;
    int b[10];
    for (i = 0; i < 10; ++i)
        b[i] = i*i;
}
```

```
i := 0 ; assignment
L1: if i >= 10 goto L2 ; conditional jump
t0 := i*i ; address-of operation
t1 := &b ; t2 holds the address of b[i]
t2 := t1 + i ; store through pointer
*t2 := t0
i := i + 1
goto L1
L2:
```

(example source: wikipedia)

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Static Single-Assignment Form (SSA)

- Every assignment writes to a distinct variable
- Every variable is only assigned once

```

p = a + b
q = p - c
p = q * d
p = e - p
q = p + q

p1 = a + b
q1 = p1 - c
p2 = q1 * d
p3 = e - p2
q2 = p3 + q1

```

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SSA

```

if (f)
  x = 42;
else
  x = 73;
y = x * a;

if (f)
  x1 = 42;
else
  x2 = 73;
x3 = φ(x1, x2);
y = x3 * a;

```

- ϕ (phi) function combines different definitions
- ϕ returns the value of x_1 if control passes through the true branch and the value of x_2 if it passed through the false branch

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SSA why should we care?

```

x = 42
x = 73
y = x

x1 = 42
x2 = 73
y = x2

```

- makes it easy to apply many optimizations
 - constant propagation, dead code elimination...

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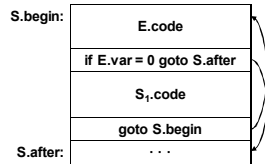
Creating 3AC: control statements

- 3AC only supports conditional/unconditional jumps
- Add labels
 - begin – label marks beginning of code
 - after – label marks end of code
- Helper function `freshLabel()` allocates a new fresh label

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Creating 3AC: control statements

$S \rightarrow \text{while } E \text{ do } S_1$



production	semantic rule
$S \rightarrow \text{while } E \text{ do } S_1$	$S.begin := \text{freshLabel}();$ $S.after := \text{freshLabel}();$ $S.code :=$ $\text{gen}(S.begin \text{'\:'}) \parallel E.code \parallel$ $\text{gen}(\text{'if' } E.var = \text{'0' } \text{'goto' } S.after) \parallel$ $S_1.code \parallel \text{gen}(\text{'goto' } S.begin) \parallel \text{gen}(S.after \text{'\:'})$

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Allocating Memory

- Type checking helped us guarantee correctness
- Also tells us
 - How much memory allocate on the heap/stack for variables
 - Where to find variables (based on offsets)
 - Compute address of an element inside array (size of stride based on type of element)

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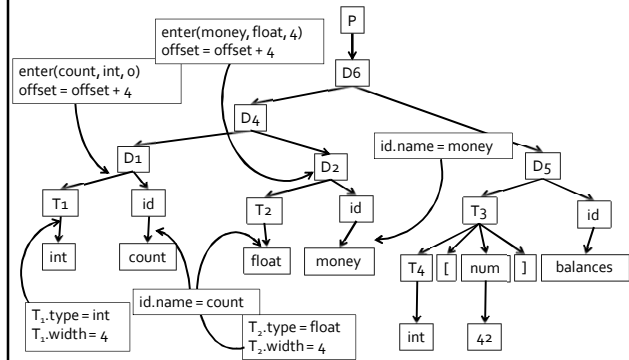
Allocating Memory

- Global variable "offset" with memory allocated so far

production	semantic rule
$P \rightarrow D$	{ offset := o }
$D \rightarrow DD$	
$D \rightarrow T \text{ id};$	{ enter(id.name, T.type, offset); offset += T.width }
$T \rightarrow \text{integer}$	{ T.type := int; T.width = 4 }
$T \rightarrow \text{float}$	{ T.type := float; T.width = 8 }
$T \rightarrow T_1[\text{num}]$	{ T.type = array (num.val, T ₁ .Type); T.width = num.val * T ₁ .width; }
$T \rightarrow *T_1$	{ T.type := pointer(T ₁ .type); T.width = 4 }

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Allocating Memory



Adjusting to bottom-up

production	semantic rule
$P \rightarrow MD$	
$M \rightarrow \epsilon$	{ offset := 0 }
$D \rightarrow DD$	
$D \rightarrow T id;$	{ enter(id.name, T.type, offset); offset += T.width }
$T \rightarrow \text{integer}$	{ T.type := int; T.width = 4 }
$T \rightarrow \text{float}$	{ T.type := float; T.width = 8 }
$T \rightarrow T_1[\text{num}]$	{ T.type = array (num.val, T ₁ .Type); T.width = num.val * T ₁ .width; }
$T \rightarrow *T_1$	{ T.type := pointer(T ₁ .type); T.width = 4 }

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Generating IR code

- Option 1
accumulate code in AST attributes
- Option 2
emit IR code to a file during compilation
 - If for every production the code of the left-hand-side is constructed from a concatenation of the code of the RHS in some fixed order

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Expressions and assignments

production	semantic action
$S \rightarrow id := E$	{ p := lookup(id.name); if p ≠ null then emit(p := E.var) else error }
$E \rightarrow E_1 \text{ op } E_2$	{ E.var := freshVar(); emit(E.var := (E ₁ .var op E ₂ .var)) }
$E \rightarrow - E_1$	{ E.var := freshVar(); emit(E.var := 'uminus' E ₁ .var) }
$E \rightarrow (E_1)$	{ E.var := E ₁ .var }
$E \rightarrow id$	{ p := lookup(id.name); if p ≠ null then E.var := p else error }

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Boolean Expressions

production	semantic action
$E \rightarrow E_1 \text{ op } E_2$	{ E.var := freshVar(); emit(E.var := 'E ₁ .var op E ₂ .var') }
$E \rightarrow \text{not } E_1$	{ E.var := freshVar(); emit(E.var := 'not' E ₁ .var) }
$E \rightarrow (E_1)$	{ E.var := E ₁ .var }
$E \rightarrow \text{true}$	{ E.var := freshVar(); emit(E.var := '1') }
$E \rightarrow \text{false}$	{ E.var := freshVar(); emit(E.var := '0') }

- Represent true as 1, false as 0
- Wasteful representation, creating variables for true/false

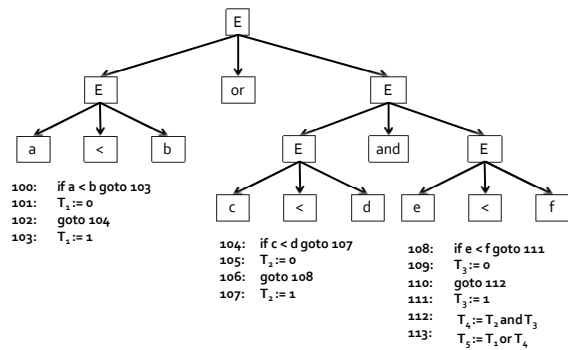
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Boolean expressions via jumps

production	semantic action
$E \rightarrow id_1 op id_2$	<pre> { E.var := freshVar(); emit('if' id1.var relop id2.var 'goto' nextStmt+2); emit(E.var := '0'); emit('goto' nextStmt+1); emit(E.var := '1') }</pre>

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Example



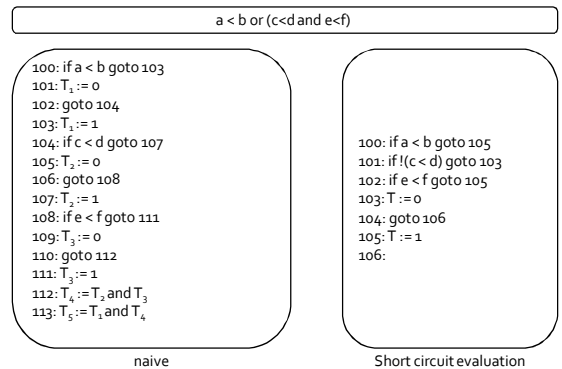
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Short circuit evaluation

- Second argument of a Boolean operator is only evaluated if the first argument does not already determine the outcome
- $(x \text{ and } y)$ is equivalent to if x then y else false;
- $(x \text{ or } y)$ is equivalent to if x then true else y

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example



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More examples

if (x != null && x.val = 42)

```
int denom = 0;
if (denom && nom/denom) {
    oops_i_just_divided_by_zero();
}
```

```
int x=0;
if (++x>0 && x++) {
    hummm ();
}
```

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Control Structures

```
S → if B then S1
    | if B then S1 else S2
    | while B do S1
```

- For every Boolean expression B, we attach two properties
 - falseLabel – target label for a jump when condition B evaluates to false
 - trueLabel – target label for a jump when condition B evaluates to true
- For every statement we attach a property
 - S.next – the label of the next code to execute after S
- Challenge
 - Compute falseLabel and trueLabel during code generation

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Control Structures: next

production	semantic action
P → S	S.next = freshLabel(); P.code = S.code label(S.next)
S → S1S2	S1.next = freshLabel(); S2.next = S.next; S.code = S1.code label(S1.next) S2.code

- Is S.next inherited or synthesized?
- Is S.code inherited or synthesized?
- The label S.next is symbolic, we will only determine its value after we finish deriving S

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Control Structures: conditional

production	semantic action
S → if B then S1	B.trueLabel = freshLabel(); B.falseLabel = S.next; S1.next = S.next; S.code = B.code gen (B.trueLabel ':') S1.code

- Are S1.next, B.falseLabel inherited or synthesized?
- Is S.code inherited or synthesized?

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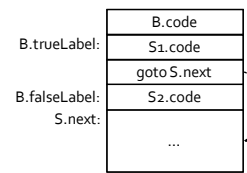
Control Structures: conditional

production	semantic action
$S \rightarrow \text{if } B \text{ then } S_1 \text{ else } S_2$	$B.\text{trueLabel} = \text{freshLabel}();$ $B.\text{falseLabel} = \text{freshLabel}();$ $S_1.\text{next} = S.\text{next};$ $S_2.\text{next} = S.\text{next};$ $S.\text{code} =$ $B.\text{code} \parallel \text{gen}(B.\text{trueLabel} ':') \parallel S_1.\text{code} \parallel \text{gen}(\text{'goto' } S.\text{next})$ $\parallel \text{gen}(B.\text{falseLabel} ':') \parallel S_2.\text{code}$

- $B.\text{trueLabel}$ and $B.\text{falseLabel}$ considered inherited

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Control Structures: conditional



```

B.trueLabel = freshLabel();
B.falseLabel = freshLabel();
S1.next = S.next;
S2.next = S.next;
S.code =
  B.code || gen(B.trueLabel ':') || S1.code || gen('goto' S.next)
  || gen(B.falseLabel ':') || S2.code
    
```

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Boolean expressions

production	semantic action
$B \rightarrow B_1 \text{ or } B_2$	$B_1.\text{trueLabel} = B.\text{trueLabel};$ $B_1.\text{falseLabel} = \text{freshLabel}();$ $B_2.\text{trueLabel} = B.\text{trueLabel};$ $B_2.\text{falseLabel} = B.\text{falseLabel};$ $B.\text{code} = B_1.\text{code} \parallel \text{gen}(B_1.\text{falseLabel} ':') \parallel B_2.\text{code}$
$B \rightarrow B_1 \text{ and } B_2$	$B_1.\text{trueLabel} = \text{freshLabel}();$ $B_1.\text{falseLabel} = B.\text{falseLabel};$ $B_2.\text{trueLabel} = B.\text{trueLabel};$ $B_2.\text{falseLabel} = B.\text{falseLabel};$ $B.\text{code} = B_1.\text{code} \parallel \text{gen}(B_1.\text{trueLabel} ':') \parallel B_2.\text{code}$
$B \rightarrow \text{not } B_1$	$B_1.\text{trueLabel} = B.\text{falseLabel};$ $B_1.\text{falseLabel} = B.\text{trueLabel};$ $B.\text{code} = B_1.\text{code};$
$B \rightarrow (B_1)$	$B_1.\text{trueLabel} = B.\text{trueLabel}; B_1.\text{falseLabel} = B.\text{falseLabel}; B.\text{code} = B_1.\text{code};$
$B \rightarrow \text{id}_1 \text{ relop id}_2$	$B.\text{code} = \text{gen}(\text{'if' id}_1.\text{var relop id}_2.\text{var 'goto' } B.\text{trueLabel}) \parallel \text{gen}(\text{'goto' } B.\text{falseLabel});$
$B \rightarrow \text{true}$	$B.\text{code} = \text{gen}(\text{'goto' } B.\text{trueLabel});$
$B \rightarrow \text{false}$	$B.\text{code} = \text{gen}(\text{'goto' } B.\text{falseLabel});$

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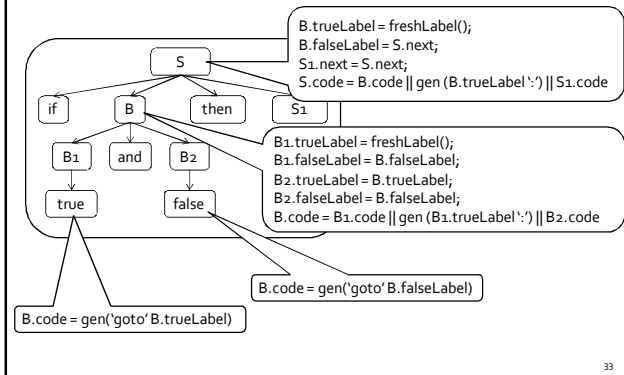
Boolean expressions

production	semantic action
$B \rightarrow B_1 \text{ or } B_2$	$B_1.\text{trueLabel} = B.\text{trueLabel};$ $B_1.\text{falseLabel} = \text{freshLabel}();$ $B_2.\text{trueLabel} = B.\text{trueLabel};$ $B_2.\text{falseLabel} = B.\text{falseLabel};$ $B.\text{code} = B_1.\text{code} \parallel \text{gen}(B_1.\text{falseLabel} ':') \parallel B_2.\text{code}$

- How can we determine the address of $B_1.\text{falseLabel}$?
- Only possible after we know the code of B_1 and all the code preceding B_1

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Example



Computing labels

- We can compute the values for the labels but it would require more than one pass on the AST
- Can we do it in a single pass?

Backpatching

- Goal: generate code in a single pass
- Generate code as we did before, but manage labels differently
- Keep labels symbolic until values are known, and then back-patch them
- New synthesized attributes for B
 - B.truelist – list of jump instructions that eventually get the label where B goes when B is true.
 - B.falselist – list of jump instructions that eventually get the label where B goes when B is false.

Backpatching

- For every label, maintain a list of instructions that jump to this label
- When the address of the label is known, go over the list and update the address of the label
- Previous solutions do not guarantee a single pass
 - The attribute grammar we had before is not S-attributed (e.g., next), and is not L-attributed.

Backpatching

- makelist(addr) – create a list of instructions containing addr
- merge(p1,p2) – concatenate the lists pointed to by p1 and p2, returns a pointer to the new list
- backpatch(p,addr) – inserts i as the target label for each of the instructions in the list pointed to by p

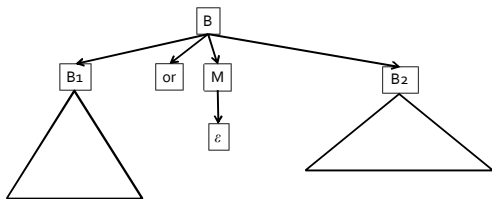
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Backpatching Boolean expressions

production	semantic action
$B \rightarrow B_1 \text{ or } M B_2$	backpatch(B1.falseList,M.instr); B.trueList = merge(B1.trueList,B2.trueList); B.falseList = B2.falseList;
$B \rightarrow B_1 \text{ and } M B_2$	backpatch(B1.trueList,M.instr); B.trueList = B2.trueList; B.falseList = merge(B1.falseList,B2.falseList);
$B \rightarrow \text{not } B_1$	B.trueList = B1.falseList; B.falseList = B1.trueList;
$B \rightarrow (B_1)$	B.trueList = B1.trueList; B.falseList = B1.falseList;
$B \rightarrow id_1 \text{ relop } id_2$	B.trueList = makeList(nextInstr); B.falseList = makeList(nextInstr+1); emit ('if' id1.var relop id2.var 'goto _') emit('goto _');
$B \rightarrow \text{true}$	B.trueList = makeList(nextInstr); emit ('goto _');
$B \rightarrow \text{false}$	B.falseList = makeList(nextInstr); emit ('goto _');
$M \rightarrow \epsilon$	M.instr = nextInstr;

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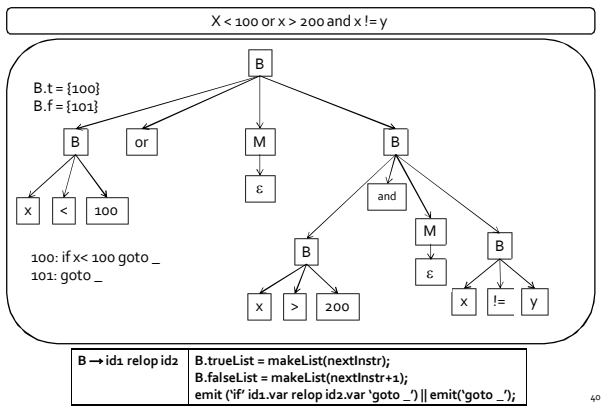
Marker



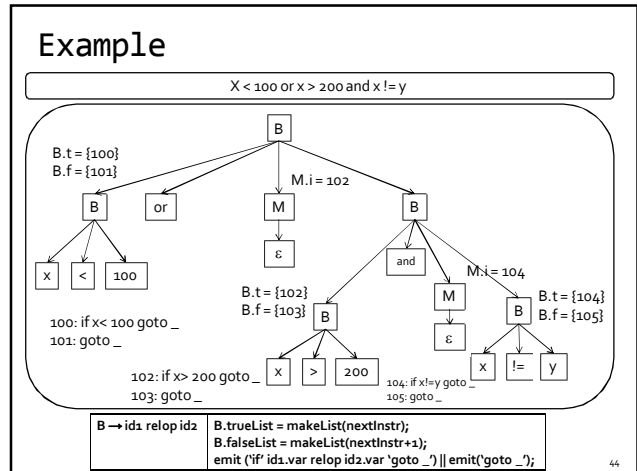
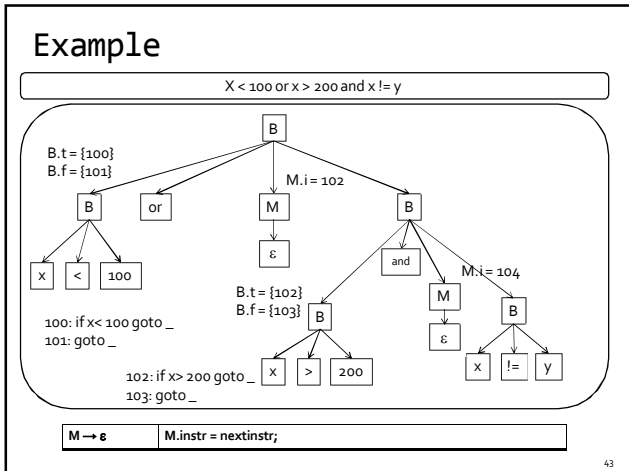
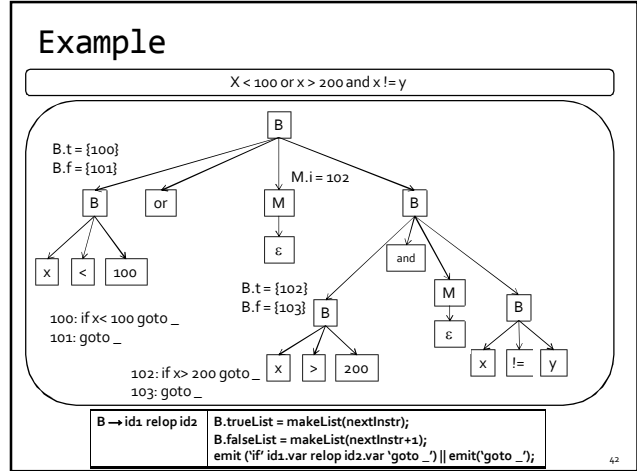
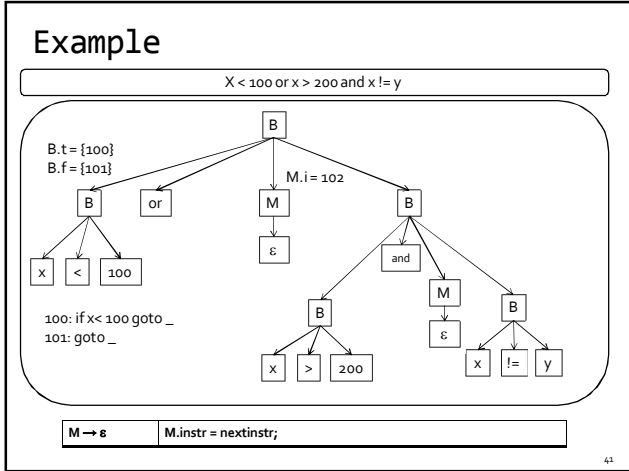
- { M.instr = nextinstr; }
- Use M to obtain the address just before B2 code starts being generated

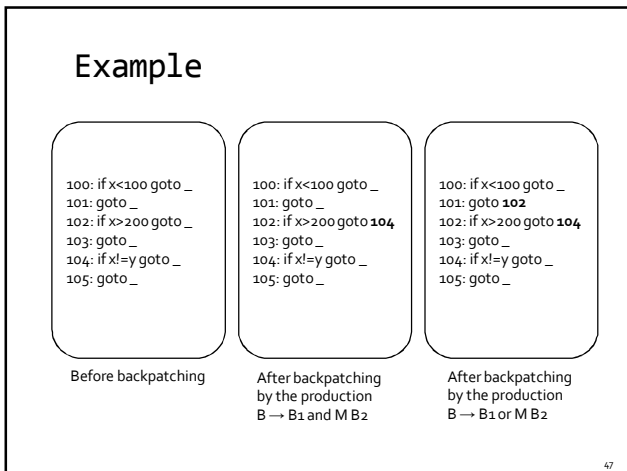
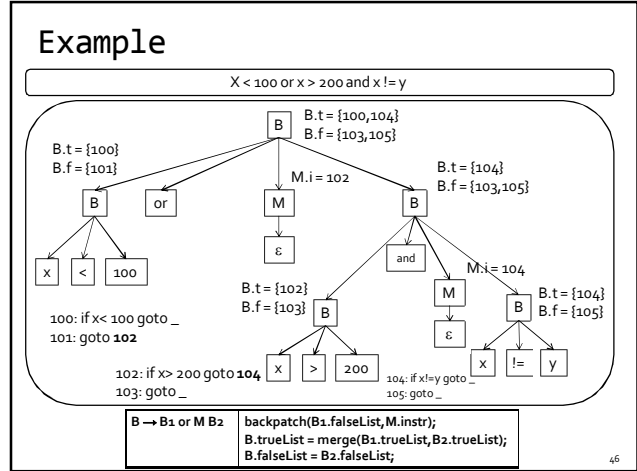
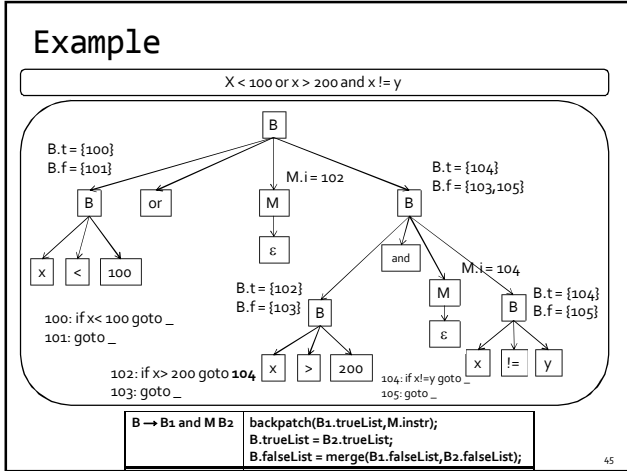
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Example



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Backpatching for statements

production	semantic action
$S \rightarrow \text{if } (B) M S_1$	$\text{backpatch}(B.\text{trueList}, M.\text{instr});$ $S.\text{nextList} = \text{merge}(B.\text{falseList}, S_1.\text{nextList});$
$S \rightarrow \text{if } (B) M_1 S_1$ $N \text{ else } M_2 S_2$	$\text{backpatch}(B.\text{trueList}, M_1.\text{instr});$ $\text{backpatch}(B.\text{falseList}, M_2.\text{instr});$ $\text{temp} = \text{merge}(S_1.\text{nextList}, N.\text{nextList});$ $S.\text{nextList} = \text{merge}(\text{temp}, S_2.\text{nextList});$
$S \rightarrow \text{while } M_1 (B)$ $M_2 S_1$	$\text{backpatch}(S_1.\text{nextList}, M_1.\text{instr});$ $\text{backpatch}(B.\text{trueList}, M_2.\text{instr});$ $S.\text{nextList} = B.\text{falseList};$ $\text{emit}(\text{'goto' } M_1.\text{instr});$
$S \rightarrow \{ L \}$	$S.\text{nextList} = L.\text{nextList};$
$S \rightarrow A$	$S.\text{nextList} = \text{null};$
$M \rightarrow \epsilon$	$M.\text{instr} = \text{nextinstr};$
$N \rightarrow \epsilon$	$N.\text{nextList} = \text{makeList}(\text{nextInstr}); \text{emit}(\text{'goto' } _);$
$L \rightarrow L_1 M S$	$\text{backpatch}(L_1.\text{nextList}, M.\text{instr});$ $L.\text{nextList} = S.\text{nextList};$
$L \rightarrow S$	$L.\text{nextList} = S.\text{nextList}$

Procedures

```
n = f(a[i]);
```

```
t1 = i * 4
t2 = a[t1] // could have expanded this as well
param t2
t3 = call f, 1
n = t3
```

- we will see handling of procedure calls in much more detail later

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Procedures

```
D → define T id (F) { S }
F → ε | T id, F
S → return E; | ...
E → id (A) | ...
A → ε | E, A
```

statements

expressions

- type checking
 - function type: return type, type of formal parameters
 - within an expression function treated like any other operator
- symbol table
 - parameter names

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Summary

- pick an intermediate representation
- translate expressions
- use a symbol table to implement declarations
- generate jumping code for boolean expressions
 - value of the expression is implicit in the control location
- backpatching
 - a technique for generating code for boolean expressions and statements in one pass
 - idea: maintain lists of incomplete jumps, where all jumps in a list have the same target. When the target becomes known, all instructions on its list are "filled in".

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Recap

- Lexical analysis
 - regular expressions identify tokens ("words")
- Syntax analysis
 - context-free grammars identify the structure of the program ("sentences")
- Contextual (semantic) analysis
 - type checking defined via typing judgements
 - can be encoded via attribute grammars
- Syntax directed translation
 - attribute grammars
- Intermediate representation
 - many possible IRs
 - generation of intermediate representation

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Journey inside a compiler

txt
position = initial + rate * 60

⇒

Token Stream

<ID,1> <=> <ID,2> <+> <ID,3> <*> <60>

Lexical Analysis

Syntax Analysis

Sem. Analysis

Inter. Rep.

Code Gen.

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Journey inside a compiler

<ID,1> <=> <ID,2> <+> <ID,3> <*> <60>

↓

symbol	type	data
position	float	...
initial	float	...
rate	float	...

AST

Lexical Analysis

Syntax Analysis

Sem. Analysis

Inter. Rep.

Code Gen.

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Journey inside a compiler

Lexical Analysis

Syntax Analysis

Sem. Analysis

Inter. Rep.

Code Gen.

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Journey inside a compiler

Intermediate Representation

```

t1 = inttofloat(60)
t2 = id3 * t1
t3 = id2 + t2
id1 = t3
                    
```

Lexical Analysis

Syntax Analysis

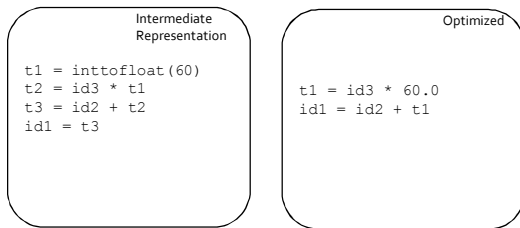
Sem. Analysis

Inter. Rep.

Code Gen.

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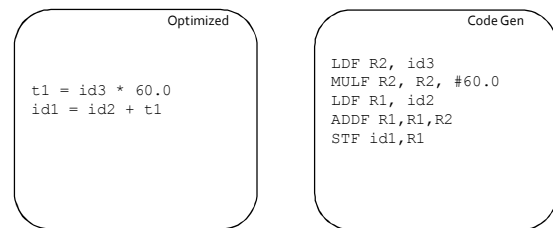
Journey inside a compiler



Lexical Analysis Syntax Analysis Sem. Analysis Inter. Rep. Code Gen.

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Journey inside a compiler



Lexical Analysis Syntax Analysis Sem. Analysis Inter. Rep. Code Gen.

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Next time

- Runtime Environments

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The End

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