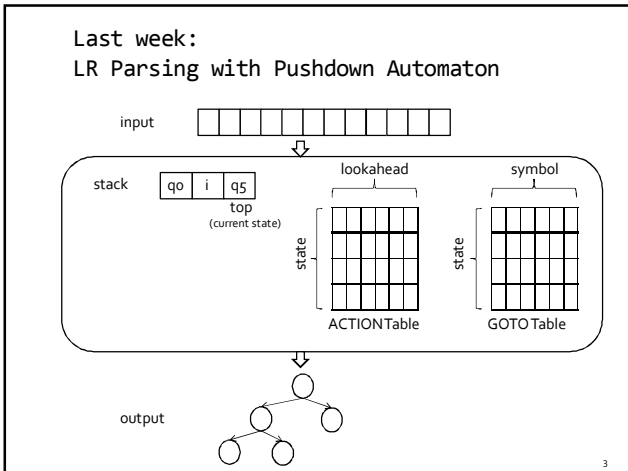
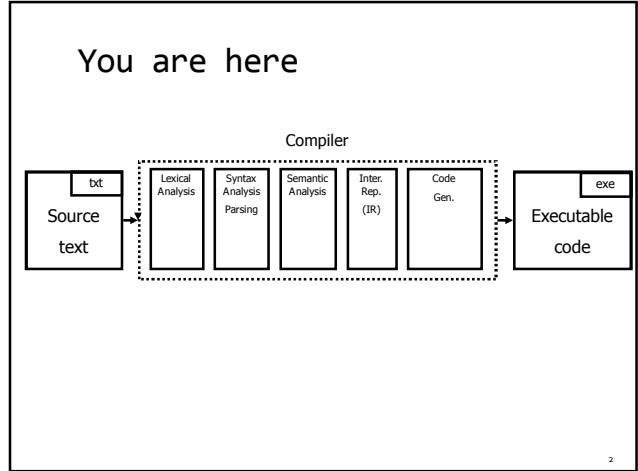


Lecture 05 – Syntax analysis & Semantic Analysis

THEORY OF COMPILATION

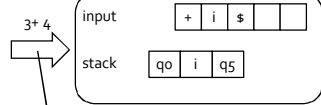
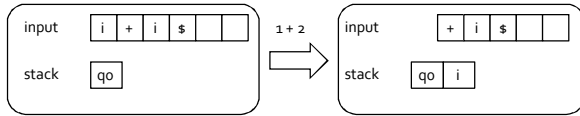
Eran Yahav

1



- Last week:
LR Parsing with Pushdown Automaton
- s = top of stack, t = next token, use ACTION[s][t] to determine what is the next move
 - Shift move
 - Remove first token t from input
 - Push t on the stack
 - Compute next state $s' = \text{GOTO}[s][t]$ table
 - Push new state s' on the stack
 - If new state is error – report error
 - Reduce move
 - Using a rule $N \rightarrow \alpha$
 - Symbols in α and their following states are removed from stack. Let q denote the state on top of stack after their removal
 - Push N on the stack
 - Compute next state $s' = \text{GOTO}[q][N]$ table
 - Push new state s' on the stack (on top of N)
- 4

Last week: shift move

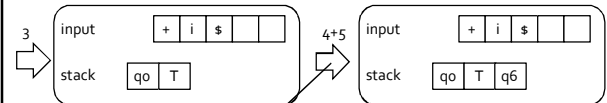
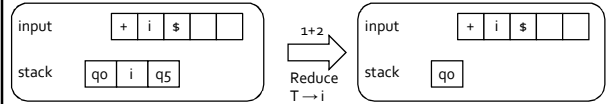


State	i	+	()	\$	E	T	action
q0	q5	q7				q1	q6	shift

1. Remove first token t from input
2. Push t on the stack
3. Compute s' = GOTO[s][t] table
4. Push s' state on the stack
5. If new state is error - report error

5

Last week: reduce move



How we picked next state

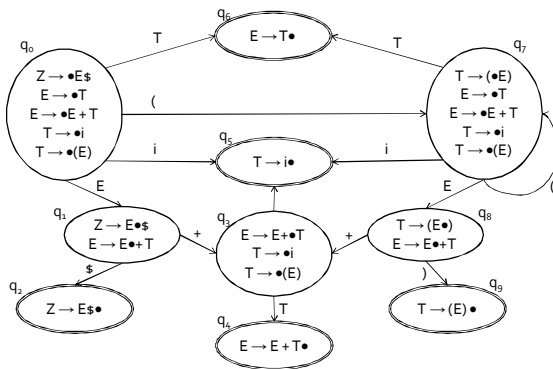
State	i	+	()	\$	E	T	action
q0	q5	q7				q1	q6	shift
...								
q5								r4

How we decided on a reduce

1. Using a rule $N \rightarrow \alpha$ (ACTION[s][t])
2. Symbols in α and their following states are removed from stack. q = top afterwards.
3. Push N on the stack
4. New state s' = GOTO[q][N] table
5. Push new state s' on top of N

6

Constructing Parse Table: LR(0) Automaton Example



7

Last week: GOTO/ACTION Table

State	i	+	()	\$	E	T
q0	s5			s7		s1	s6
q1		s3			s2		
q2	r1	r1	r1	r1	r1	r1	r1
q3	s5			s7			s4
q4	r3	r3	r3	r3	r3	r3	r3
q5	r4	r4	r4	r4	r4	r4	r4
q6	r2	r2	r2	r2	r2	r2	r2
q7	s5			s7		s8	s6
q8		s3		s9			
q9	r5	r5	r5	r5	r5	r5	r5

- (1) $Z \rightarrow E \$$
- (2) $E \rightarrow T$
- (3) $E \rightarrow E + T$
- (4) $T \rightarrow i$
- (5) $T \rightarrow (E)$

Warning: numbers mean different things!
 m = reduce using rule number n
 sm = shift to state m

8

LR Parsing with Pushdown Automaton (superimposed GOTO/ACTION)

- s = top of stack, t = next token, $\text{move} = \text{GOTO/ACTION}[s][t]$ to determine what is the next move
- If (move = Sm)
 - Remove first token t from input
 - Push t on the stack
 - Push new state m on the stack
- If (move = rn)
 - use rule number $n: N \rightarrow \alpha$
 - Symbols in α and their following states are removed from stack. Let q denote the state on top of stack after their removal
 - Push N on the stack
 - Compute next state $s' = \text{GOTO/ACTION}[q][N]$ table
 - Push new state s' on the stack (on top of N)
- If (move = empty) report ERROR

9

GOTO/ACTION Table

st	i	+	()	\$	E	T
q0	s5		s7			s1	s6
q1		s3			s2		
q2	r1	r1	r1	r1	r1	r1	r1
q3	s5		s7				s4
q4	r3	r3	r3	r3	r3	r3	r3
q5	r4	r4	r4	r4	r4	r4	r4
q6	r2	r2	r2	r2	r2	r2	r2
q7	s5		s7			s8	s6
q8		s3			s9		
q9	r5	r5	r5	r5	r5	r5	r5

- (1) $Z \rightarrow E \$$
- (2) $E \rightarrow T$
- (3) $E \rightarrow E + T$
- (4) $T \rightarrow i$
- (5) $T \rightarrow (E)$

top is on the right

Stack	Input	Action
q0	i + i \$	s5
q0 i q5	+ i \$	r4
q0 T q6	+ i \$	r2
q0 E q1	+ i \$	s3
q0 E q1 + q3	i \$	s5
q0 E q1 + q3 i q5	\$	r4
q0 E q1 + q3 T q4	\$	r3
q0 E q1	\$	s2
q0 E q1 \$ q2		r1
q0 Z		

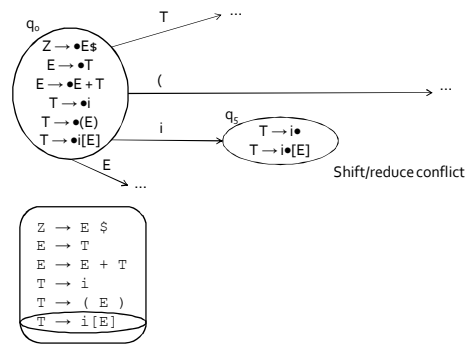
10

Are we done?

- Can make a transition diagram for any grammar
- Can make a GOTO table for every grammar
- Cannot make a deterministic ACTION table for every grammar

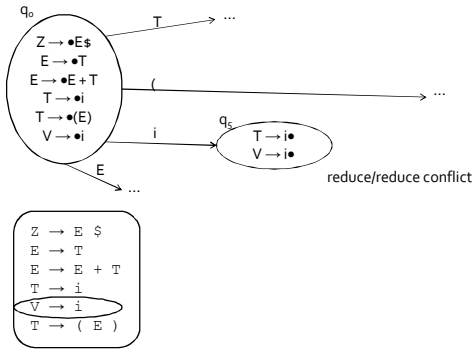
11

LR(0) Conflicts



12

LR(0) Conflicts



13

LR(0) Conflicts

- Any grammar with an ϵ -rule cannot be LR(0)
- Inherent shift/reduce conflict
 - $A \rightarrow \epsilon \bullet$ - reduce item
 - $P \rightarrow \alpha \bullet A \beta$ - shift item
 - $A \rightarrow \epsilon \bullet$ can always be predicted from $P \rightarrow \alpha \bullet A \beta$

14

Back to the GOTO/ACTIONS tables

State	GOTO Table						action	
	i	+	()	\$	T		
q0	q5		q7			q1	q6	shift
q1		q3			q2			shift
q2								$Z \rightarrow E \$$
q3	q5		q7				q4	Shift
q4								$E \rightarrow E + T$
q5								$T \rightarrow i$
q6								$E \rightarrow T$
q7	q5		q7			q8	q6	shift
q8		q3		q9				shift
q9								$T \rightarrow E$

ACTION table determined only by transition diagram, ignores input

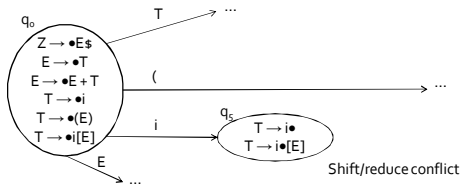
15

SLR Grammars

- Don't reduce if it will get you into trouble on the next token
- A handle should not be reduced to a non-terminal N if the look-ahead is a token that cannot follow N
- A reduce item $N \rightarrow \alpha \bullet$ is applicable only when the look-ahead is in FOLLOW(N)
- Differs from LR(0) only on the ACTION table

16

LR(0) Conflicts



Z	→	E	\$
E	→	T	
E	→	E + T	
T	→	i	
T	→	(E)	
T	→	i [E]	

A(x)	\$	input
------	----	-------

FOLLOW(Z)	=	{ \$ }
FOLLOW(E)	=	{) + \$ }
FOLLOW(T)	=	{) + \$ }

17

SLR ACTION Table

State	i	+	()	\$
q0	shift		shift		
q1		shift			shift
q2					Z→E\$
q3	shift		shift		
q4		E→E+T		E→E+T	E→E+T
q5		T→i		T→i	T→i
q6		E→T		E→T	E→T
q7	shift		shift		
q8		shift		shift	
q9		T→(E)		T→(E)	T→(E)

Look-ahead token from the input

Remember: In contrast, GOTO table is indexed by state and a grammar symbol from the stack

- (1) Z → E \$
 - (2) E → T
 - (3) E → E + T
 - (4) T → i
 - (5) T → (E)
-
- | | | |
|-----------|---|------------|
| FOLLOW(Z) | = | { \$ } |
| FOLLOW(E) | = | {) + \$ } |
| FOLLOW(T) | = | {) + \$ } |

18

SLR ACTION Table

missing rules

State	i	+	()	[]	\$
q0	shift		shift				
q1		shift					shift
q2							Z→E\$
q3	shift		shift				
q4		E→E+T		E→E+T			E→E+T
q5		T→i		T→i	shift		T→i
q6		E→T		E→T			E→T
q7	shift		shift				
q8		shift		shift			
q9		T→(E)		T→(E)			T→(E)

SLR - use 1 token look-ahead

... as before...
T → i
T → i [E]

FOLLOW(Z)	=	{ \$ }
FOLLOW(E)	=	{) + \$ }
FOLLOW(T)	=	{) + \$ }

19

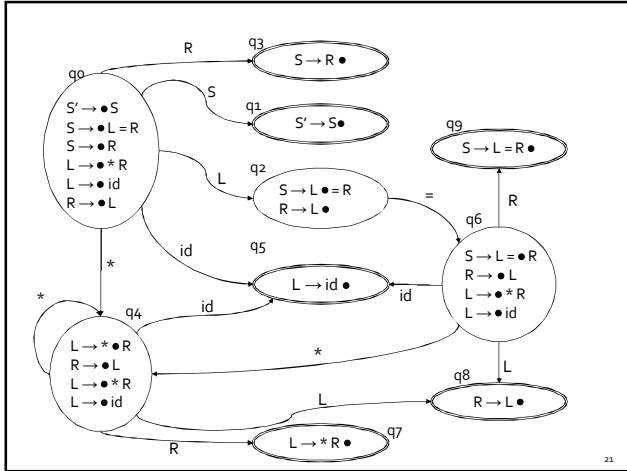
LR(0) - no look-ahead

state	action
q0	shift
q1	shift
q2	Z→E\$
q3	Shift
q4	E→E+T
q5	T→i
q6	E→T
q7	shift
q8	shift
q9	T→E

Are we done?

- (0) S' → S
- (1) S → L = R
- (2) S → R
- (3) L → * R
- (4) L → id
- (5) R → L

20



Shift/reduce conflict

(0) $S' \rightarrow S$
 (1) $S \rightarrow L = R$
 (2) $S \rightarrow R$
 (3) $L \rightarrow * R$
 (4) $L \rightarrow id$
 (5) $R \rightarrow L$

q2

$S \rightarrow L = R$
 $R \rightarrow L \bullet$

=

$S \rightarrow L = \bullet R$
 $R \rightarrow \bullet L$
 $L \rightarrow \bullet * R$
 $L \rightarrow \bullet id$

- $S \rightarrow L = \bullet R$ vs. $R \rightarrow L \bullet$
- FOLLOW(R) contains =
 - $S \Rightarrow L = R \Rightarrow * R = R$
- SLR cannot resolve the conflict either

LR(1) Grammars

- In SLR: a reduce item $N \rightarrow \alpha \bullet$ is applicable only when the look-ahead is in FOLLOW(N)
- But FOLLOW(N) merges look-ahead for all alternatives for N
- LR(1) keeps look-ahead with each LR item
- Idea: a more refined notion of follows computed per item

LR(1) Item

- LR(1) item is a pair
 - LR(0) item
 - Look-ahead token
- Meaning
 - We matched the part left of the dot, looking to match the part on the right of the dot, followed by the look-ahead token.
- Example
 - The production $L \rightarrow id$ yields the following LR(1) items

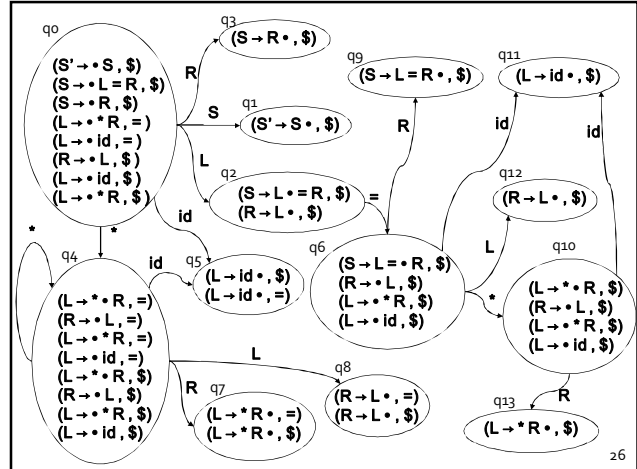
(0) $S' \rightarrow S$
 (1) $S \rightarrow L = R$
 (2) $S \rightarrow R$
 (3) $L \rightarrow * R$
 (4) $L \rightarrow id$
 (5) $R \rightarrow L$

$[L \rightarrow \bullet id, *]$
 $[L \rightarrow \bullet id, =]$
 $[L \rightarrow \bullet id, id]$
 $[L \rightarrow \bullet id, \$]$
 $[L \rightarrow id \bullet, *]$
 $[L \rightarrow id \bullet, =]$
 $[L \rightarrow id \bullet, id]$
 $[L \rightarrow id \bullet, \$]$

ϵ -closure for LR(1)

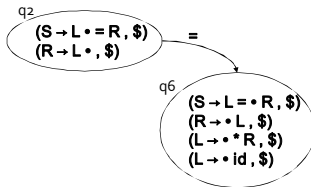
- For every $[A \rightarrow \alpha \bullet B\beta, c]$ in S
 - for every production $B \rightarrow \delta$ and every token b in the grammar such that $b \in \text{FIRST}(\beta c)$
 - Add $[B \rightarrow \bullet \delta, b]$ to S

25



26

Back to the conflict



- Is there a conflict now?

27

LALR

- LR tables have large number of entries
- Often don't need such refined observation (and cost)
- LALR idea: find states with the same LR(0) component and merge their look-ahead component as long as there are no conflicts
- LALR not as powerful as LR(1)

28

Summary: LR Grammars

- LR parsing techniques use item sets of proposed handles
 - Shift behavior similar
 - Differ on when to reduce
- LR(0) - any reduce item causes a reduction
- SLR – a reduce item $N \rightarrow \alpha \bullet$ causes a reduction only if the look-ahead token is in the FOLLOW set of N
- LR(1) - a reduce item $N \rightarrow \alpha \bullet \{ \sigma \}$ causes a reduction only if the look-ahead token is in the set σ (the look-ahead set computed for the item)

29

Summary: LR Grammars

- ACTION table determines whether to shift or reduce
- On a shift, new state found using the GOTO table
- LR-parser with 1 token look-ahead, the ACTION and GOTO tables can be superimposed

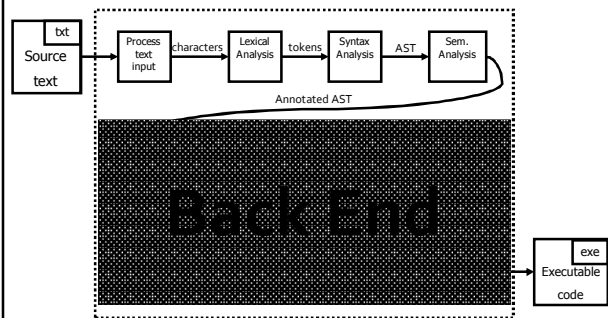
30

Summary

- Bottom up
 - LR Items
 - LR parsing with pushdown automata
 - LR(0), SLR, LR(1) – different kinds of LR items, same basic algorithm

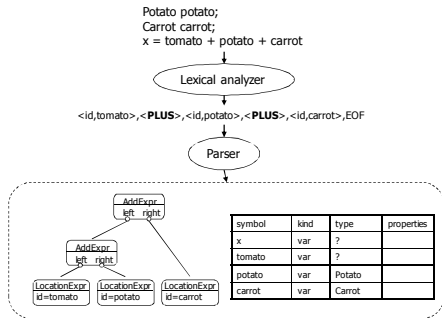
31

You are here...



32

What we want



tomato is undefined
 potato used before initialized
 Cannot add Potato and Carrot

33

Syntax vs. Semantics

- Syntax
 - Program structure
 - Formally described via context free grammars
- Semantics
 - Program meaning
 - Formally defined as various forms of semantics (e.g., operational, denotational)
 - It is actually NOT what "semantic analysis" phase does
 - Better name – "contextual analysis"

34

Contextual Analysis

- Often called "Semantic analysis"
- Properties that cannot be formulated via CFG
 - Type checking
 - Declare before use
 - Identifying the same word "w" re-appearing – wbw
 - Initialization
 - ...
- Properties that are hard to formulate via CFG
 - "break" only appears inside a loop
 - ...
- Processing of the AST

35

Abstract Syntax Tree (AST)

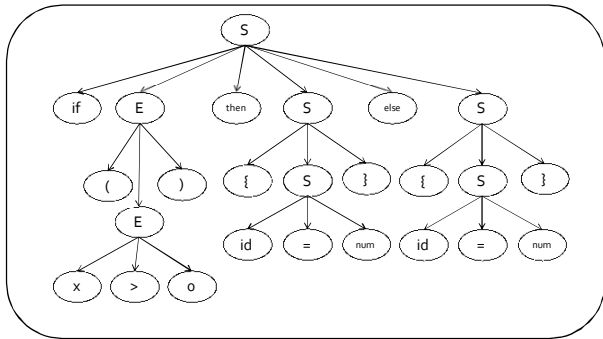
- Abstract away some syntactic details of the source language

S → if E then S else S
 | ...

```
if (x>0)
then { y = 42 }
else { y = 73 }
```

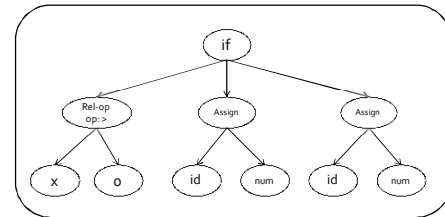
36

Parse tree (concrete syntax tree)



37

Abstract Syntax Tree (AST)



38

Syntax Directed Translation

- Semantic attributes
 - Attributes attached to grammar symbols
- Semantic actions
 - (already mentioned when we did recursive descent)
 - How to update the attributes
- Attribute grammars

39

Attribute grammars

- Attributes
 - Every grammar symbol has attached attributes
 - Example: Expr.type
- Semantic actions
 - Every production rule can define how to assign values to attributes
 - Example:

$$\text{Expr} \rightarrow \text{Expr} + \text{Term}$$

$$\text{Expr.type} = \text{Expr}_1.\text{type} \text{ when } (\text{Expr}_1.\text{type} == \text{Term.type})$$

$$\text{Error otherwise}$$

40

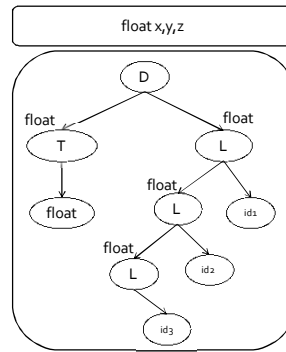
Indexed symbols

- Add indexes to distinguish repeated grammar symbols
- Does not affect grammar
- Used in semantic actions

- $Expr \rightarrow Expr + Term$
 Becomes
 $Expr \rightarrow Expr_1 + Term$

41

Example



Production	Semantic Rule
$D \rightarrow T L$	$L.in = T.type$
$T \rightarrow int$	$T.type = integer$
$T \rightarrow float$	$T.type = float$
$L \rightarrow L_1, id$	$L_1.in = L.in$ $addType(id.entry, L.in)$
$L \rightarrow id$	$addType(id.entry, L.in)$

42

Dependencies

- A semantic equation $a = b_1, \dots, b_m$ requires computation of b_1, \dots, b_m to determine the value of a

- The value of a depends on b_1, \dots, b_m
 - We write $a \leftarrow b_i$

43

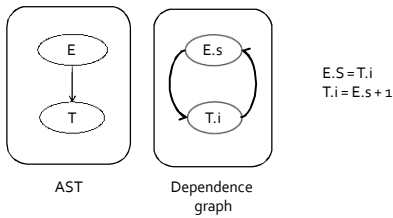
Attribute Evaluation

- Build the AST
- Fill attributes of terminals with values derived from their representation
- Execute evaluation rules of the nodes to assign values until no new values can be assigned
 - In the right order such that
 - No attribute value is used before its available
 - Each attribute will get a value only once

44

Cycles

- Cycle in the dependence graph
- May not be able to compute attribute values



45

Attribute Evaluation

- Build the AST
- Build dependency graph
- Compute evaluation order using topological ordering
- Execute evaluation rules based on topological ordering
- Works as long as there are no cycles

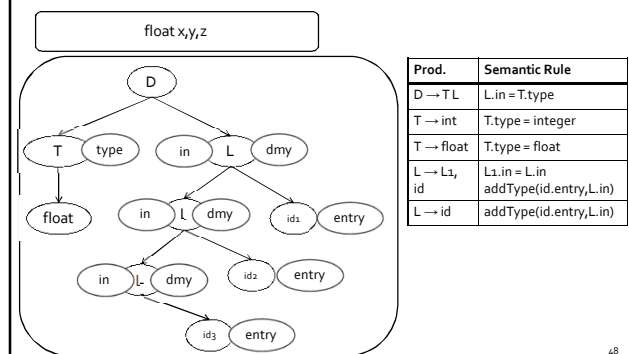
46

Building Dependency Graph

- All semantic equations take the form
 $attr1 = func1(attr1.1, attr1.2, \dots)$
 $attr2 = func2(attr2.1, attr2.2, \dots)$
- Actions with side effects use a dummy attribute
- Build a directed dependency graph G
 - For every attribute a of a node n in the AST create a node n.a
 - For every node n in the AST and a semantic action of the form $b = f(c_1, c_2, \dots, c_k)$ add edges of the form (c_i, b)

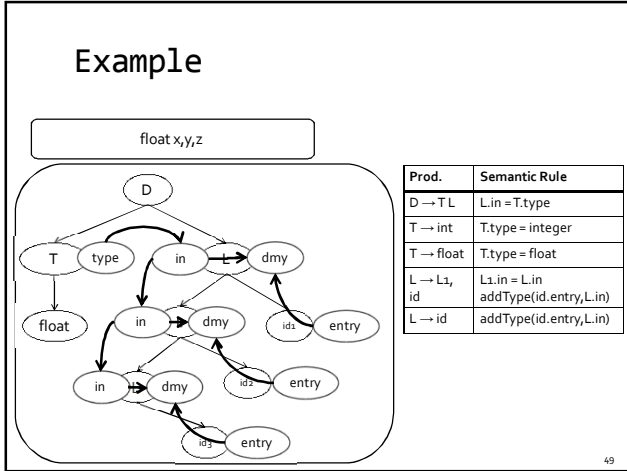
47

Example



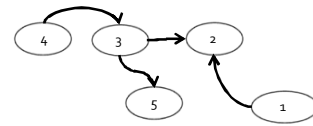
48

Example



Topological Order

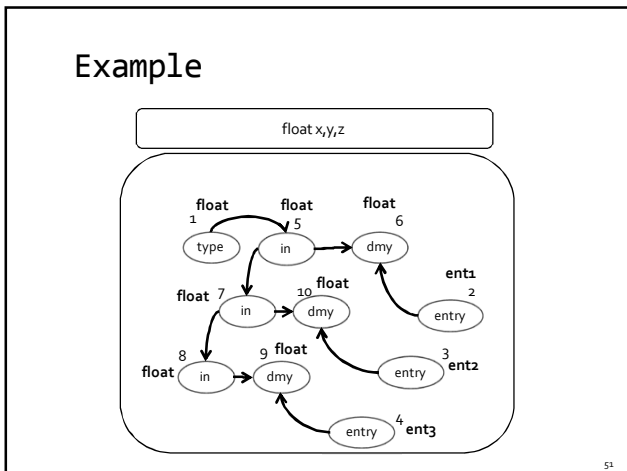
- For a graph $G=(V,E), |V|=k$
- Ordering of the nodes v_1, v_2, \dots, v_k such that for every edge $(v_i, v_j) \in E, i < j$



Example topological orderings: 1 4 3 2 5, 4 1 3 5 2

50

Example



But what about cycles?

- For a given attribute grammar hard to detect if it has cyclic dependencies
 - Exponential cost
- Special classes of attribute grammars
 - Our "usual trick"
 - sacrifice generality for predictable performance

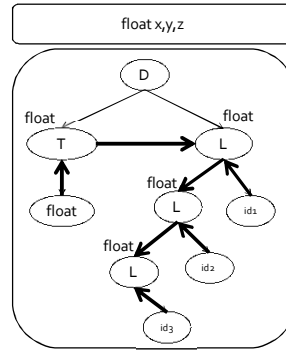
52

Inherited vs. Synthesized Attributes

- Synthesized attributes
 - Computed from children of a node
- Inherited attributes
 - Computed from parents and siblings of a node
- Attributes of tokens are technically considered as synthesized attributes

53

example



Production	Semantic Rule
$D \rightarrow T L$	$L.in = T.type$
$T \rightarrow int$	$T.type = integer$
$T \rightarrow float$	$T.type = float$
$L \rightarrow L_1, id$	$L_1.in = L.in$ $addType(id.entry, L.in)$
$L \rightarrow id$	$addType(id.entry, L.in)$

→ inherited
→ synthesized

54

S-attributed Grammars

- Special class of attribute grammars
- Only uses synthesized attributes (S-attributed)
- No use of inherited attributes
- Can be computed by any bottom-up parser during parsing
- Attributes can be stored on the parsing stack
- Reduce operation computes the (synthesized) attribute from attributes of children

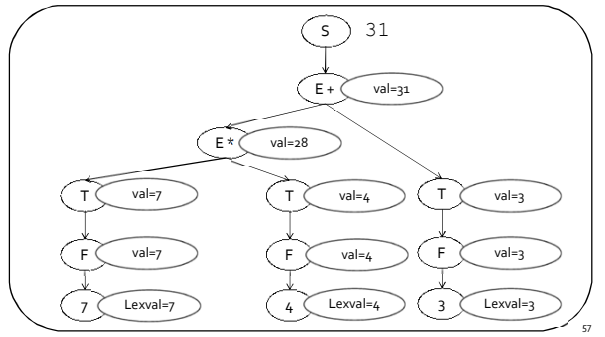
55

S-attributed Grammar: example

Production	Semantic Rule
$S \rightarrow E;$	$print(E.val)$
$E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
$E \rightarrow T$	$E.val = T.val$
$T \rightarrow T_1 * F$	$T.val = T_1.val * F.val$
$T \rightarrow F$	$T.val = F.val$
$F \rightarrow (E)$	$F.val = E.val$
$F \rightarrow digit$	$F.val = digit.lexval$

56

example



57

L-attributed grammars

- L-attributed attribute grammar when every attribute in a production $A \rightarrow X_1 \dots X_n$ is
 - A synthesized attribute, or
 - An inherited attribute of X_j , $1 \leq j \leq n$ that only depends on
 - Attributes of $X_1 \dots X_{j-1}$ to the left of X_j , or
 - Inherited attributes of A

58

Summary

- Contextual analysis can move information between nodes in the AST
 - Even when they are not "local"
- Attribute grammars
 - Attach attributes and semantic actions to grammar
- Attribute evaluation
 - Build dependency graph, topological sort, evaluate
- Special classes with pre-determined evaluation order: S-attributed, L-attributed

59

The End

60

Identification

61

Scopes

62

Semantic Checks

- Scope rules
 - Use symbol table to check that
 - Identifiers defined before used
 - No multiple definition of same identifier
 - Program conforms to scope rules
- Type checking
 - Check that types in the program are consistent
 - How?

63

Type Checking

- Type rules specify
 - which types can be combined with certain operator
 - Assignment of expression to variable
 - Formal and actual parameters of a method call
- Examples

```

string      string
"drive" + "drink"
      string
int         string
42 + "the answer"
      ERROR

```

64

Type Checking Rules

- Specify for each operator
 - Types of operands
 - Type of result
- Basic Types
 - Building blocks for the type system (type rules)
 - e.g., int, boolean, string
- Type Expressions
 - Array types
 - Function types
 - Record types / Classes

65

Typing Rules

If E1 has type int and E2 has type int,
then E1 + E2 has type int

$$\frac{E1 : \text{int} \quad E2 : \text{int}}{E1 + E2 : \text{int}}$$

(Generally, also use a context A)

66

More Typing Rules

$$\frac{}{A \vdash \text{true} : \text{boolean}} \quad \frac{}{A \vdash \text{false} : \text{boolean}}$$

$$\frac{}{A \vdash \text{int-literal} : \text{int}} \quad \frac{}{A \vdash \text{string-literal} : \text{string}}$$

$$\frac{A \vdash E1 : \text{int} \quad A \vdash E2 : \text{int}}{A \vdash E1 \text{ op } E2 : \text{int}} \quad \text{op} \in \{ +, -, /, *, \% \}$$

$$\frac{A \vdash E1 : \text{int} \quad A \vdash E2 : \text{int}}{A \vdash E1 \text{ rop } E2 : \text{boolean}} \quad \text{rop} \in \{ <=, <, >, >= \}$$

$$\frac{A \vdash E1 : T \quad A \vdash E2 : T}{A \vdash E1 \text{ rop } E2 : \text{boolean}} \quad \text{rop} \in \{ ==, != \}$$

67

And Even More Typing Rules

$$\frac{A \vdash E1 : \text{boolean} \quad A \vdash E2 : \text{boolean}}{A \vdash E1 \text{ lop } E2 : \text{boolean}} \quad \text{lop} \in \{ \&\&, || \}$$

$$\frac{A \vdash E1 : \text{int}}{A \vdash ! E1 : \text{boolean}} \quad \frac{A \vdash E1 : \text{boolean}}{A \vdash ! E1 : \text{boolean}}$$

$$\frac{A \vdash E1 : T[]}{A \vdash E1.length : \text{int}} \quad \frac{A \vdash E1 : T[] \quad A \vdash E2 : \text{int}}{A \vdash E1[E2] : T} \quad \frac{A \vdash E1 : \text{int}}{A \vdash \text{new } T[E1] : T[]}$$

$$\frac{A \vdash T \setminus \text{in } C}{A \vdash \text{new } T() : T} \quad \frac{\text{id} : T \in A}{A \vdash \text{id} : T}$$

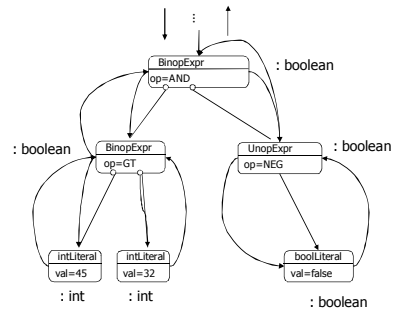
68

Type Checking

- Our approach --- Traverse AST bottom-up and assign types for AST nodes
 - Use typing rules to compute node types
- More complicated alternative --- type-check during parsing
 - But naturally also more efficient

69

Example



45 > 32 && !false

$$\frac{}{A :- E1 : \text{boolean} \quad A :- E2 : \text{boolean}}$$

$$\frac{A :- E1 \quad \text{lop} E2 : \text{boolean}}{A :- E1 \quad \text{lop} E2 : \text{boolean}}$$

lop ∈ { &&, || }

$$\frac{A :- E1 : \text{boolean}}{A :- !E1 : \text{boolean}}$$

$$\frac{A :- E1 : \text{int} \quad A :- E2 : \text{int}}{A :- E1 \quad \text{rop} E2 : \text{boolean}}$$

rop ∈ { <=, <, >, >= }

$$\frac{}{A :- \text{false} : \text{boolean}}$$

$$\frac{}{A :- \text{int-literal} : \text{int}}$$

70