

Graph parameters and graph polynomials: Definability and complexity

Course given in Prague, 2014, in the DOC-COURSE series

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Graph polynomial project:
<http://www.cs.technion.ac.il/~janos/RESEARCH/gp-homepage.html>

Outline of the course

LECTURE 00: Second Order Logic (SOL) and its fragments (Background, not lectured)
LOGICS (14 slides)

LECTURE 01: Friday, Oct 10, 2014, 14:00-15:40, Prague Lecture 1,
A landscape of graph parameters and graph polynomials. Comparing graph parameters.
Towards a general theory.
(90 minutes, 90 slides with skip-options)

LECTURE 02: Thursday, Oct 16, 2014, 12:20-14:00 Prague Lecture 2,
Why is the chromatic polynomial a polynomial? Where to graph polynomial occur
naturally? Definability of graph properties and graph polynomials in fragment of Second
Order Logic.
(90 minutes, ca. 99 slides with skip options)

LECTURE 03: Thursday, Oct 16, 2014, 14:30-16:00 Prague Lecture 3,
Connection matrices for graph parameters. When do connection matrices of graph
parameters have finite rank? Connection matrices for graph parameters definable in
fragments of Second Order Logic. The finite rank theorem. Using connections matrices
to prove non-definability.
(90 minutes, ca. 55 slides with skip options)

Further links to the literature.

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Further links

- [arXiv] J.A. Makowsky's Graph Polynomial [Go to Homepage](http://www.cs.technion.ac.il/~janos/RESEARCH/gp-homepage.html) at <http://www.cs.technion.ac.il/~janos/RESEARCH/gp-homepage.html>
- [KMR 2013] J. A. Makowsky T. Kotek and E. V. Ravve, [A computational framework for the study of partition functions and graph polynomials](#). In Proceedings of the 12th Asian Logic Conference '11, pages 210-230, 2013. [download](http://www.cs.technion.ac.il/~janos/RESEARCH/alcpaper.pdf) at <http://www.cs.technion.ac.il/~janos/RESEARCH/alcpaper.pdf>
- [GKM 2012] B. Godlin, E. Katz and J. A. Makowsky, [Graph Polynomials: From Recursive Definitions to Subset Expansion Formulas](#). J. Log. Comput. 22(2): 237-265 (2012) [download](http://www.cs.technion.ac.il/~janos/RESEARCH/GodlinKatzMakowsky.pdf) at <http://www.cs.technion.ac.il/~janos/RESEARCH/GodlinKatzMakowsky.pdf>
- [M 2008] J.A. Makowsky, [From a Zoo to a Zoology: Towards a general theory of graph polynomials](#), Theory of Computing Systems, 2008. [download](http://dx.doi.org/10.1007/s00224-007-9022-9) at <http://dx.doi.org/10.1007/s00224-007-9022-9>

More links

[File:p-overview.tex](#)

Further links, II

[arXiv] J.A. Makowsky's **papers** at http://arxiv.org/find/all/1/au:+Makowsky/0/1/0/all/0/1?per_page=100 on **arXiv**.

[dblp] J.A. Makowsky's **papers** at http://www.informatik.uni-trier.de/~ley/pers/hd/m/Makowsky:Johann_A=.html on **DBLP**.

[google] J.A. Makowsky's **papers** at http://scholar.google.co.il/citations?hl=en&user=ooNKL6UAAAAJ&pagesize=100&view_op=list_works at **scholar.google**.

[Course notes] J.A. Makowsky's **Course notes**.

[PhD Theses] **PhD Theses** on graph polynomials (a selection)

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Further links: Course notes

Slides of courses on graph polynomials and related topics:

Technion 2005/6 [Lecture notes](#) of **Advanced Topics in Computer Science (238900)**

Technion 2009/10 [Lecture notes](#) of **Advanced Topics in Computer Science (236605)**

Vienna 2014 [Lecture notes](#) of **EMCL Lecture 2014: Graph polynomials**

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Further links: PhD Theses

PhD Theses on graph polynomials and related topics:

- I. Averbuch** [PhD Thesis](#) (Technion 2011): [Completeness and Universality Properties of Graph Invariants and Graph Polynomials](#)
- T. Kotek** [PhD Thesis](#) (Technion 2012): [Definability of combinatorial functions](#)
- M. Trinks** [PhD Thesis](#) (TU Freiberg 2012): [Graph Polynomials and Their Representations](#)

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