On the direction of fibring feature logics with concatenation logics*

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Abstract

A dual-fibring of a feature-logic and a concatenation-logic is proposed, in which syntactic categorial types “live in” feature terms, in contrast to current fibring, in which feature-terms “live in” types. The dual-fibring contains also arrow-introduction rules for hypothetical reasoning. It is used to explain some “privileged features” in HPSG and their non-unification manipulation.

Keywords: Feature-Logic, Lambek-calculus, unification, fibring, categorial-grammar, natural language

1 Introduction

Recent advances in the ‘parsing as deduction’ paradigm are advocating the combination of two logics, a “concatenation-logic” and a “feature-logic”, as the adequate means of implementing this paradigm, in view of the advent of ‘unification-based grammar-formalisms’. Two recent examples of this approach are [3] and [4]. The combination of the logics is called ‘fibring’ in [3], and we retain this name generically in this paper. Both papers consider the Lambek logic \( L \) [5] as the concatenation-logic, but differ in several respects regarding the way \( L \) should be fibred with a feature-logic:

1. Should the operators of \( L \) be applied directly to atomic elements of the feature-logic, or should the latter be embedded within atomic \( L \)-types (as arguments)?
2. Should the feature-logic be based on unification or on subsumption?
3. Should the restrictions imposed by the feature-logic be localized (to derivation-steps), or kept globally?

However, one common implicit assumption in both approaches is, that in the fibring (in spite of its symmetric definition w.r.t. the fibred logics), the feature-logic should be embedded within the concatenation-logic, no matter how the above differences are to be resolved. Thus, the focus is on extended-types, in such a way that feature information “lives-within” types. In particular, this view induces a role of feature information as a partitioning of types into subtypes, or a refinement of

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the type-structure. For example, the basic type *np* (denoting noun-phrases) can be partitioned into \(^1 np(num : sg)\) and \(np(num : pl)\), denoting, respectively, singular and plural noun-phrases.

In this paper, a dual-fibring is proposed, that embeds the concatenation-logic within the feature-logic, by which categorial information is made to “live-within” feature-terms. It seems that this kind of dual-fibring fits better the practice of grammar writers, in particular in the HPSG framework [7], and explains the role of “privileged features” such as ‘cat’, ‘subcat’, ‘dtrs’ etc., a role stipulated in HPSG without any theoretical justification, except for the clear linguistic need and adequacy of its use. Often, such privileged features have values the manipulation of which exceeds unification, again, without an explicit justification. The latter phenomenon is mentioned in [8] (p. 295) as a general characteristic of many unification-based grammar-formalisms. The dual-fibring suggested here may constitute a common explanation and justification for many such “deviations” from unification, and explains the privileged features as arising from the interface-rules used in the fibring of two logics, while the role from unification in handling the values of these features reflects the proof-rules of the concatenation-logic. This view induces a dual role of features and types; the types are now seen as partitioning feature-structures (or refining them) according to categorial information. For example, the class of feature-structures satisfying (in AVM-notation) \(T = [vform : finite]\), denoting all entities with a finite verb-form feature, can be partitioned into \(T[np \to s]\) and \(T[np \to (s \leftarrow np)]\), denoting, respectively intransitive verbs (or object-saturated verb-phrases) and transitive verbs. Here \(T[A]\) denotes an encoding of an extended-type (explained below) as a sub-feature-term within a feature-term \(T\). The resulting logic has a lot in common with CUG ([2], [1]). However, it is, according to the classification of [6], a second-generation logic, due to the presence of residiuation-rules for hypothetical reasoning, while CUG is classified as first-generation system in the absence of such rules. It still remains to be investigated what is the logic arising when neither of the entities “lives-within” the other, applying the fully-recursive definition of fibring as given in [3]. Many simplifications are assumed in the current paper. The uncovering of the fibred-logics structure of “full HPSG” remains an issue for further research.

2 The base-logics

The following definitions are basically extracted from [3].

The feature-term logic

The syntax of FL (over a signature \(\langle F, P \rangle\) of feature-names and node-predicate-names, respectively) is described in Figure 1. Terms of the feature-logic FL are interpreted over feature-structures \(A = (D^A, \{f^A|f \in F\}, \{p^A|p \in P\})\), where: \(D^A\) is a non-empty set of nodes, for each \(f \in F\), \(f^A\) is a partial function on \(D^A\), and for each \(p \in P\), \(p^A\) is a subset of \(D^A\). The satisfaction of an FL term \(T\) over a feature structure \(A\) w.r.t. a variable assignment \(g\) (taking care of reentrancy), denoted by \(\langle A, g, d\rangle \models_{FL} T\), is presented in Figure 2. A term \(T_2\) is an FL-consequence of a term \(T_1\), denoted by \(T_1 \models_{FL} T_2\), iff for all \(A, g, d\): if \(\langle A, g, d\rangle \models_{FL} T_1\), then \(\langle A, g, d\rangle \models_{FL} T_2\).

\(^1\)In the introduction, the notation is supposed to be self-explanatory. It is properly introduced in the body of the paper.
The concatenation logic

As for the concatenation logic, we also consider $\mathcal{L}$, Lambek’s basic logic, over a set $B$ of basic types. The syntax of $\mathcal{L}$ is given in Figure 3. Terms of $\mathcal{L}$ (types) are interpreted over string structures (models) $(\mathcal{S}, \delta)$, consisting of a non-empty set $S$ (“words”), and an interpretation that assigns to each basic category $b \in B$ a non-empty set $b^S \subseteq S^+$ (strings over $S$). The denotations of syntactic types are presented in Figure 4. The deductive calculus is defined over (declarative) units $U \triangleright A$, where $U$ keeps track of the resource management over assumptions in proofs. The proof-rules are presented in Figure 5. The reader is referred to [3] for the definition of the fibred logic $\mathcal{L}(FL)$, the fibred structure over which this logic is interpreted, and a complete calculus for deriving valid declarative units.

3 The dual-fibring logic

In this section, we show how to dual-fiber the concatenation-logic $\mathcal{L}$ into the feature-terms logic FL. The dual-fibred logic is referred to as FL($\mathcal{L}$), in analogy with the fibering $\mathcal{L}(FL)$ in [3]. The corresponding calculus is also based on fibering satisfiability of feature-terms with validity of types, as in the usual fibrings. For the interface-rules of the dual-fibring, we assume that $\{cat, lsubcat, rsubcat, dtrs, hdtr, cdtr\} \cap \mathcal{F} = \emptyset$, and extend the $\mathcal{F}$-component of the signature of FL($\mathcal{L}$) by these feature-names. The first three features accommodate the directionality of $\mathcal{L}$-types similarly to the
\[ [b]_S = b \]
\[ [C \to B]_S = \{ \tau \forall \tau' \in [C]_S \tau \tau' [B]_S \} \]
\[ [B \leftarrow C]_S = \{ \tau \forall \tau' \in [C]_S \tau \tau' [B]_S \} \]

Figure 4: The denotation of \( \mathcal{L} \)-types

\[
\begin{align*}
(ax) \quad & A \triangleright A \\
(\to E) \quad & \frac{U_1 \triangleright B \quad U_2 \triangleright (B \to A)}{U_1 \triangleright (B \Rightarrow B) \triangleright A} \\
(\to I) \quad & \frac{U \triangleright (B \Rightarrow A)}{U \triangleright (B \Rightarrow A)}
\end{align*}
\]

Figure 5: The type calculus for \( \mathcal{L} \)

way \( \text{subcat} \) and \( \text{cat} \) act\(^2\) in HPSG. Similarly, the last three encode the hierarchical structure of signs (strings), similarly to the use of the \( \text{DTRS} \) (daughters), head-daughter and complement daughter in HPSG. As we are simplifying a lot here, the special role of heads is not fully reflected. The functor is the head, and the argument - the complement (in the right linear-order imposed by the directionality of the functor). In addition, we assume that \( \mathcal{P} \cap \mathcal{B} = \emptyset \), and extend the \( \mathcal{P} \)-component of the signature with the elements of \( \mathcal{B} \) as new sort-names.

For defining the syntax of \( \text{FL}(\mathcal{L}) \), we use some auxiliary definitions. Wherever convenient, we use the AVM-notation for feature terms. First, \( \text{extended types} \) are defined by extending the arrow-operators to feature-terms encoding type on top of some other information. Let \( T \) be an \( \text{FL} \)-term and \( b \in \mathcal{B} \).

\[ EA \rightarrow T[b] \mid T[EA_1 \to EA_2] \mid T[EA_2 \leftarrow EA_1] \]

With each extended-type \( EA \) we can naturally associate its underlying \( \mathcal{L} \)-type, “stripping” all its feature information, so to speak, denoted \( \tau(EA) \), by letting

\[ \tau(EA) = \begin{cases} 
\tau(EA_1) \to \tau(EA_2) & EA = T[EA_1 \to EA_2] \\
\tau(EA_2) \leftarrow \tau(EA_1) & EA = T[EA_2 \leftarrow EA_1] 
\end{cases} \]

We use a \textit{type-extension} \( T[EA] \) for denoting the extension of a feature-term \( T \) with an extended type \( EA \), defined by \( T[EA] =_{\text{ar}} T \cup \theta[EA] \), where \( \theta[EA] \) is a function encoding\(^3\) an extended-type as an \( \text{FL}(\mathcal{L}) \)-term, using the new feature-names and new type-sorts in the extended signature, defined as follows:

\[
\theta[EA] =_{\text{ar}} \begin{cases} 
T \cup \{ \text{cat} : b \} & \text{EA} = T[b] \\
T \cup \{ \text{cat} : \theta[EA_2] \} & \text{EA} = T[EA_1 \to EA_2] \\
T \cup \{ \text{cat} : \theta[EA_1] \} & \text{EA} = T[EA_2 \leftarrow EA_1] 
\end{cases}
\]

By this construction, the categorial information “lives-within” feature-terms as desired, leaving the denotation of type-extended feature-terms to be a feature-structure. The dependence on the embedded categorial type is reflected in the definition of the validity of a declarative-unit as defined below, and in the preservation of

\(^2\)We ignore here multiple complements on the subcat list in HPSG, and consider a “binary version” of it. Also, we ignore here HPSG’s multiple valency lists. A full exposition of HPSG as a fibred logic should deal with both issues.

\(^3\)Similarly to the encoding in CUG ([2], [1]).
this validity by the rules of the FL(Ł)-calculus presented in the sequel. This specific
day of encoding types allows feature-information everywhere, not only in conjunction
with basic types, or heads. The linguistic motivation for such encodings may be
found in [2] and [1]. For example, assuming that \{num, pers, v form, s form\} ⊆ F,
\{sg, 3rd, fin, affirm\} ⊆ P and \{np, s\} ⊆ B, and letting \(T_1 = \begin{bmatrix}
\text{num} : & \text{sg} \\
\text{pers} : & \text{3rd}
\end{bmatrix}\),
\(T_2 = \begin{bmatrix}
\text{form} : & \text{affirm}
\end{bmatrix}\) and \(T_3 = \begin{bmatrix}
\text{form} : & \text{affirm}
\end{bmatrix}\), we have:

\[T_3[T_1[np] \rightarrow T_2[s]] = \begin{bmatrix}
\text{cat} : & \text{v form} : \text{affirm} \\
\text{subcat} : & \text{pers} : \text{3rd} \\
\text{v form} : & \text{fin}
\end{bmatrix}
\]
as an FL(Ł)-term. Note that it has feature information at all levels. Under this
view, lexical entries assigned to words are extended-types.

Before embarking on the full presentation of FL(Ł), we make a small detour to
explain more of HPSG’s privileged features. One can make a distinction between
two kinds of logics expressing grammars: recognition-logics and parsing-logics. In
a recognition logic, derivability of a suitable term signals membership of a certain
string in the language defined by the grammar encoded by the logic. However, no
extra information about the member string is present. On the other hand, in a
parsing-logic, the derived term expresses (in addition to membership in the lan-
guage) some syntactic structure attributed to the member string by the grammar,
e.g., a phrase-structure. This reflects the known distinction between weak gener-
ating power and strong generative power; usually, the latter is of more interest in
computational linguistics.

As it turns out, the role of HPSG’s features like ‘DT RS’ (daughters), ‘HD TR’
(head-daughter), ‘CD TRS’ (complement-daughters) and the like, is an encoding of
the information needed for a parsing-logic. In defining a dual-fibering for that
purpose, we use \(\delta(T[EA], T_1[EA_1], T_2[EA_2])\) to denote the hierarchical embedding
of two (type-extended) feature terms \(T_1, T_2\) in (the type-extended) feature-term \(T\),
using the daughters features. Thus,

\[\delta(T[EA], T_1[EA_2 \leftarrow EA_1], T_2[EA_1]) = \text{df}\ T[EA] \sqcup \left[ \begin{array}{c}
\text{hdr} : & T_1[EA_2 \leftarrow EA_1] \\
\text{cdtr} : & T_2[EA_1]
\end{array} \right]\]

To maintain a simpler notation, we focus in the rest of this paper on a dual-fibering
variant of FL(Ł) reflecting a recognition-logic only. The extension to a full parsing-
logic is not hard. Thus, the syntax of FL(Ł) consists of type-extended feature terms
\(T[EA]\) as defined above.

We now turn to the denotation of FL(Ł)-terms and declarative-units. Both are
interpreted in dual-fibred structures \(\mathcal{M} = (S, \Lambda, g, \{R_b\}_{b \in B})\), where \(S\) is a string-
model, \(\Lambda\) a feature-structure, \(g\) a variable-assignment \(\mathcal{V} \rightarrow \mathcal{D}^\Lambda\), and \(R_b \subseteq \mathcal{D}^\Lambda \times b^\Sigma\) is a family (indexed by basic types) of fibring-relations \(^4\), such that whenever
\(\Lambda, g, d = \text{cat} : b\) (for some \(b \in B\)), there exists some string \(\tau \in S^+\) such that \(dR_b \tau\).

The denotation \([T[EA]]^\mathcal{M}\) of an FL(Ł)-term \(T[EA]\) has already been fixed via
satisfaction in \(\mathcal{A}\). To take the categorial type into account, we associate with every

\(^4\)Note the difference in the direction of the relation compared to the fibring-relations in [3].
Note that by this definition we have for every \( \text{FL}(L) \)-term \( T[E] \) and \( \mathcal{M} \)

\[
L[T[E]]^\mathcal{M} \subseteq [\tau(T[E])]^\mathcal{M}.
\]

As for the denotation of the resources ("structured databases"), these are a natural extension of feature-structures called multi-rooted structures (MRSs), described in detail in [9]. Basically, these are sequences of feature-structures with possible sharing (reentrancy) of substructures between elements of a sequence. We use sequences of \( \text{FL}(L) \)-terms (with possibly shared variables) to denote them. The definition of the language associated with a type-extended feature-term is naturally extended by letting

\[
L[T_1[E_1], T_2[E_2]]^\mathcal{M} =_{df} L[T_1[E_1]]^\mathcal{M} \cdot L[T_2[E_2]]^\mathcal{M}.
\]

namely, the concatenation (in \( S^+ \)) of the respective languages. Note that by this definition, the inclusion of languages to the denotations of the underlying type is preserved, i.e.,

\[
L[T_1[E_1], T_2[E_2]]^\mathcal{M} \subseteq [\tau(T_1[E_1], T_2[E_2])]^\mathcal{M}.
\]

Finally, a declarative-unit \((U_1, \ldots, U_m) \triangleright T[E]\) is valid iff for all dual-fibred structures \( \mathcal{M} \),

\[
L[(U_1, \ldots, U_m)]^\mathcal{M} \subseteq L[T[E]]^\mathcal{M}.
\]

Following the HPSG convention, we represent also the lexical input words (and the generated concatenations thereof) as the value of yet another (new) feature, \textit{phon}.

For the presentation of the fibred calculus, we use \( u(T_1, T_2) \) to denote that the (satisfiable) \( \text{FL}(L) \)-terms \( T_1, T_2 \) are unifiable, and \( T_1 \sqcup T_2 \) for the (satisfiable) outcome of their unification. The form of an axiom now becomes as follows.

\[
\frac{T}{T[E] \triangleright T[E]}
\]

meaning that the type-extension of a satisfiable term with any extended type derives itself. The new form of the elimination rule \( \leftarrow E \) now becomes:

\[
\frac{(\leftarrow E) \quad U_1 \triangleright T_1[T_1, T_2] \leftarrow T_1, U_2 \triangleright T_2[E_2, T_1, T_2], u(T_1, T_2), u(T_1, T_2, T_2, E_2) \quad (U_1, U_2) \triangleright \sqcup (T_1, T_2)[E_2, T_1, T_2]}{(U_1, U_2) \triangleright \sqcup (T_1, T_2)[E_2, T_1, T_2]}
\]

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5Only rooted, connected, finite feature-structures are considered in [9], but all definitions extend naturally to the more relaxed definition employed here.
The primes indicate the feature-terms after the side-effect of unification. The unifiability requirement is a side-condition of the rule, and is placed as assumptions for notational convenience only. This rule reflects a simplified version of the subcategorization-principle, as well as the head-feature principle of HPSG.

In Figure 7 is a sample derivation of a highly simplified representation for Mary loves John, where the only syntactic restriction present is number-agreement between the subject and the verb. To save space, the feature names ‘rsubcat’ and ‘lsubcat’ are abbreviated to ‘rsub’ and ‘lsub’, respectively.

Next, we turn to the new form of a residuation-rule. The feature percolations for such rules are not explicitly discussed in the literature. The main property of the new form of the residuation-rules is, that feature-information present in the assumption is preserved, to be made use of after the discharge of the assumption. The new form of the \((\leftarrow I)\) rule is as follows.

\[
(\leftarrow I) \quad (U, T_1 [EA_1]) \triangleright T_2 [EA_2] \\
U \triangleright T_2 (E_i \leftarrow T_1 [EA_1])
\]

To exemplify the particular feature percolation employed by the rule, we consider in the next section an example from Hebrew. The full calculus is presented in Figure 8. The following lemma ensures the soundness of the FL(\(\mathcal{L}\))-calculus, based on the soundness of the \(\mathcal{L}\)-calculus.

**Lemma:** (type-restriction)
If \(U_i, \ i = 1, n\) are satisfiable, and \(\vdash_{FL(\mathcal{L})} (U_1, \ldots, U_m) \triangleright T[EA]\), then \(T[EA]\) is satisfiable, and furthermore, \(\vdash_{\mathcal{L}} (\tau(U_1), \ldots, \tau(U_m)) \triangleright \tau(T[EA])\).

**Proof:** By a simple inductive argument on the structure of proofs. Satisfiability is preserved by the proof-rules due to the unifiability tests. The inclusion of the associated languages in the denotations of the underlying types was observed before, and the proof-rule mimic the categorial manipulation of these languages.
4 An application of residuation

First, recall the derivation of John whom Mary likes slept in [3], using the residuation rule \((\leftarrow I)\) of \(\mathcal{L}\). The category assigned to whom is \((np \rightarrow np) \leftarrow (s \leftarrow np)\), which triggers the introduction of an assumption \([np]_1\) (with a null string value), later discharged by the residuation rule. We now show how the corresponding \(FL(\mathcal{L})\) rule can be used to solve elegantly a generalization of relativizing in English.

In Hebrew, many categories, including NPs, VPs and APs, are marked for gender, being either feminine or masculine. In particular, according to some syntactic analysis\(^6\) of Hebrew, there are two relative pronouns of the two corresponding genders, \(ota\) (feminine) and \(oto\) (masculine), similarly to German and Russian, for example. One of the agreement rules in Hebrew calls for a gender agreement between a relative pronoun (in a relative clause), and the relativized NP (in addition to subject-verb gender agreement). Note that the first person singular pronoun \(any\) (i.e., \(I\)) is underspecified for gender, and agrees with both genders. Thus, we have\(^7\):

1. \(hayeled\) oto ani ohev shar
   namely
   the boy\(_m\) whom\(_m\) I love\(_m\) sings\(_m\),
   but
2. \(^*\) \(hayalda\) oto ani ohev shar
   namely
   \(^*\) the girl\(_f\) whom\(_m\) I love\(_m\) sings\(_f\).
   Similarly,
3. \(hayalda\) ota ani ohev shar
   namely
   the girl\(_f\) whom\(_f\) I love\(_m\) sings\(_f\),
   but
4. \(^*\) \(hayeld\) ota ani ohev shar
   namely
   \(^*\) the boy\(_m\) whom\(_f\) I love\(_m\) sings\(_m\).

\(^6\) Other analyses regard these examples as having a phonologically-empty relative-pronoun, and a dislocated resumptive pronoun.

\(^7\) To simplify, we ignore the fact that Hebrew is written from right to left.
Actually, as there are also plural versions of these relative pronouns (otam for masculine-plural and ota for feminine-plural), we end up in four similar, though different, lexical entries. Let us ignore for this example all other featural distinctions as number, person, etc., as well as their agreement rules. One way of enforcing the gender agreement in relativization is to assign the following extended categories to oto and ota, using a gender feature gen with atomic values m (for masculine) and f (for feminine). This way, the specific gender expected by each relative pronoun is built-in in its lexical entry.

The generated assumption now carries gender information, that has to be percolated when a residuation-rule is applied (otherwise this information disappears with the discharged assumption). Figure 9 shows the main part of the derivation corresponding to hayeled oto ani ohev shar. The rest of the derivation combines with the subject, matching the masculine gender, and then the relativized NP combines with the intransitive verb sings, again with the right gender agreement.

Note that the lexical value associated with the verbs ohev/ohvet right-subcategorizes for a (gender-underspecified) np, being ready to combine with noun-phrases of both genders. The gender of the generated assumption “dictates” the way the derivation proceeds. A similar derivation exists for (3), where the generated assumption has $\text{gen} : f$ as the extra-categorial initial feature-information, to match that assigned to ota. On the other hand, there is no way to generate assumptions that will cause the wrong gender matching with the relative pronoun, thus blocking (4) and (2). The structure of the above derivation can be viewed as a logical counterpart of a typical use of the SLASH feature in HPSG’s treatment of object relativization. Similar use of hypothetical reasoning in other cases of long-distance dependencies suggests itself.
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